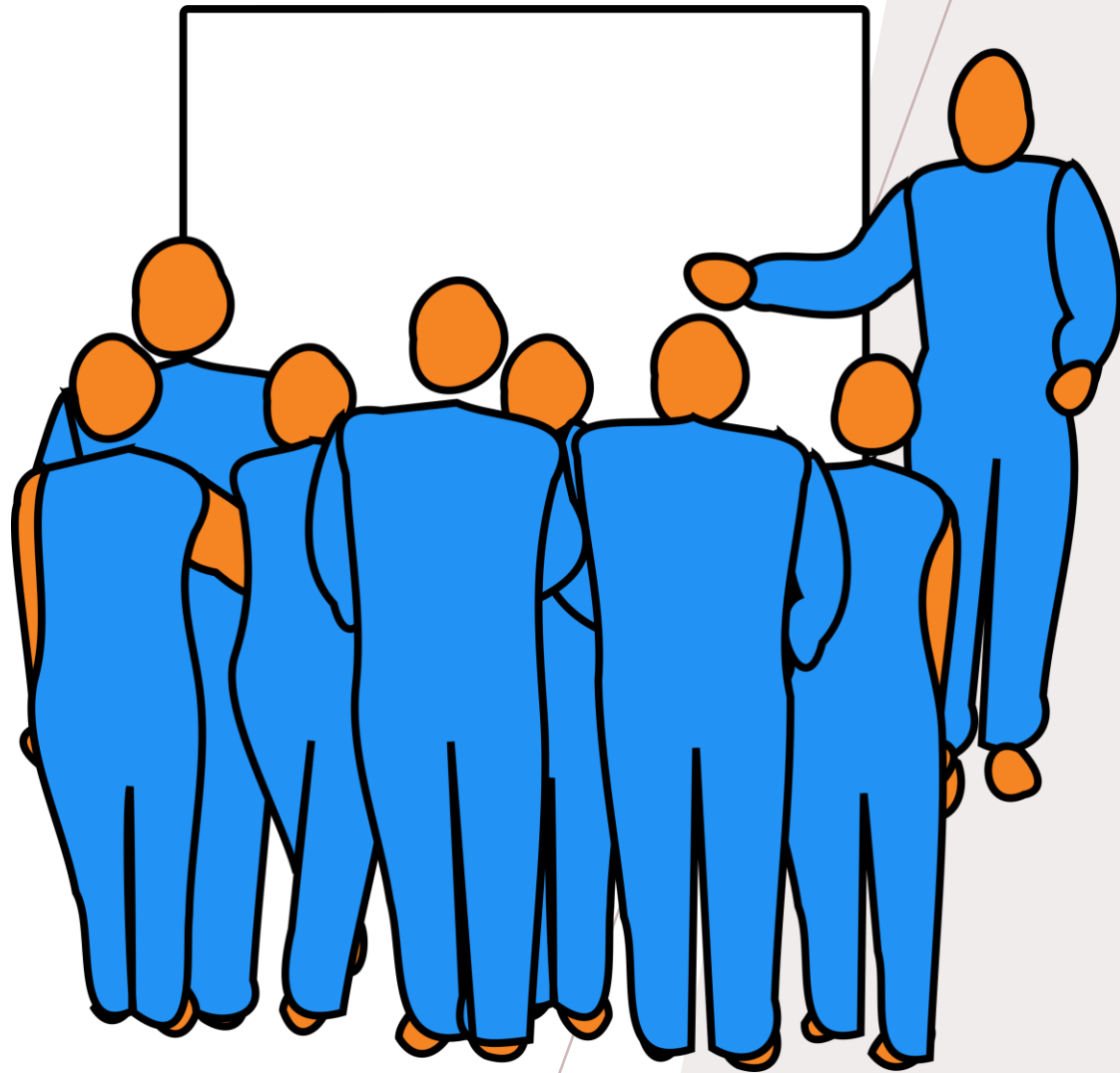




JOURNAL CLUB

07 November 2025

Presenter

Paballo Adelina Khotso

Msc. Medical Epidemiology



Joining the Dots: Linking Disconnected Networks of Evidence Using Dose-Response Model-Based Network Meta-Analysis

Hugo Pedder^{}, Sofia Dias^{}, Meg Bennetts, Martin Boucher, and Nicky J. Welton

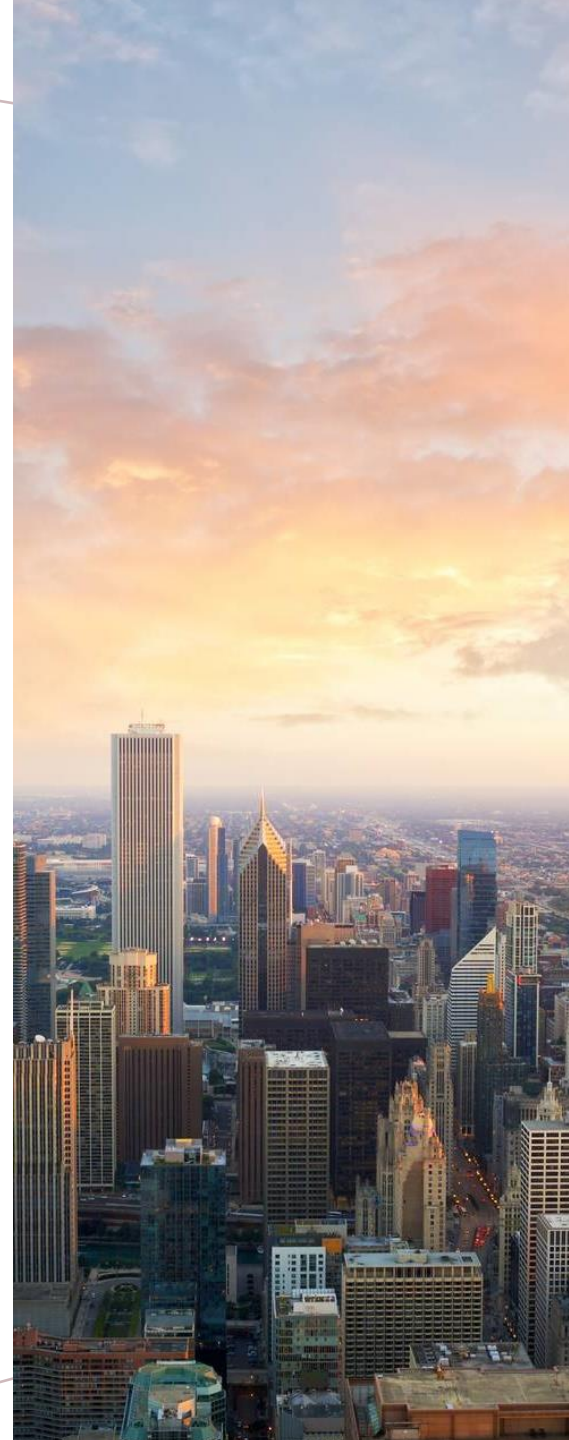
Introduction

Methods

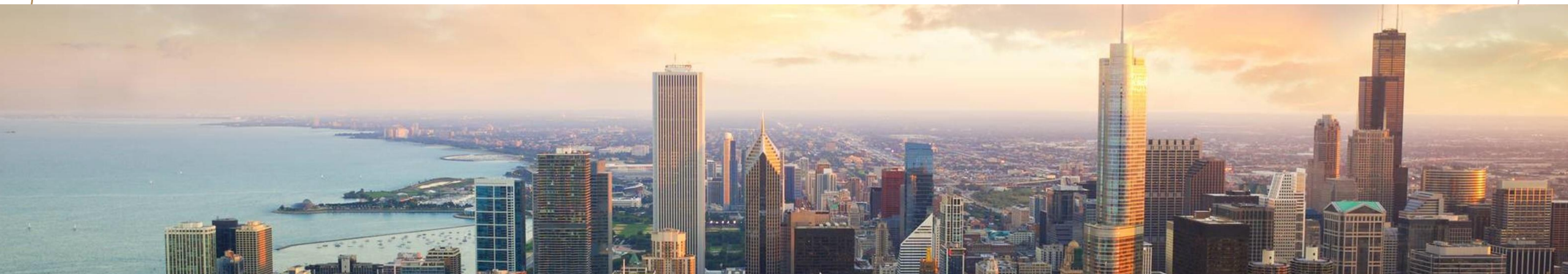
Results

Discussion

Conclusion



INTRODUCTION

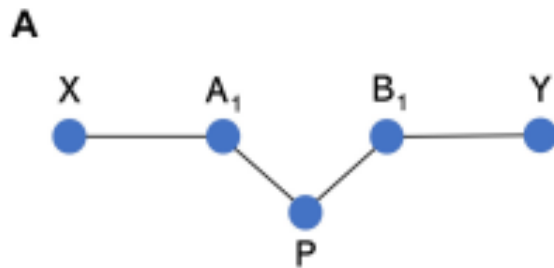


BACKGROUND

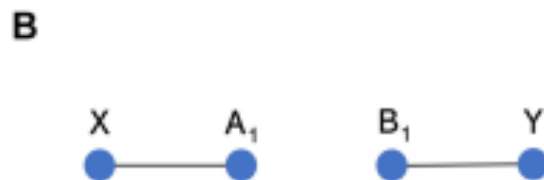
- Health care policy decisions use cost effectiveness analysis to support decision making of health professionals
- Estimating the relative effectiveness of multiple treatments options is an important element.
- Typically done by network meta-analysis

NETWORK META-ANALYSIS (NMA)

- Method of pooling the results of primary studies to enable a comparison of multiple treatments options simultaneously.
- Provided that they form a connected network of treatment comparisons.



A. Connected Network



B. Disconnected Network

DISCONNECTED NETWORKS IN NMA

- Make it impossible to obtain relative effect estimates of disconnected treatment comparisons
- Or lead to estimation of very imprecise relative effects.

B



HOW TO DEAL WITH DISCONNECTED NETWORKS IN NMA

METHODS





METHODS

1. Use of observational or registry data
2. Evidence in other populations
3. Expert opinion
4. Population adjustment methods
5. Hierarchical models
6. Modeling intervention components

EXAMPLES

1. Using Evidence in other populations

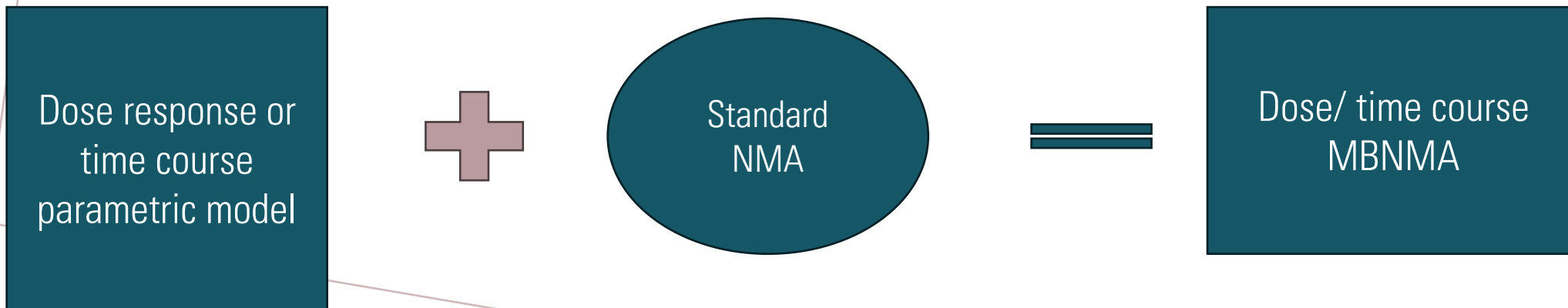
- In a study comparing treatments for plaque psoriasis in **children and young people**.
- Adalimumab was disconnected from the network
- Evidence from an adult trial was used to connect the NMA comparing the treatments of interest.

2. Using observational data and population adjustment methods.

- Study for relapsed and refractory multiple myeloma
- There was no RCT evidence connecting pomalidomide with comparators panobinostat or bendamustine.
- Analysis of individual patient data from single arms and population adjustment methods were used to connect the network.
- However, **all these methods make strong and typically untestable assumptions**

MODEL-BASED NETWORK META-ANALYSIS (MBNMA)

- **New methodology** that has the potential to connect networks
- By using evidence on
- Multiple doses of 1 or more agents (**dose response**)
- Observations at multiple follow-up times (**time course**)
- And still preserves randomization of included RCTs

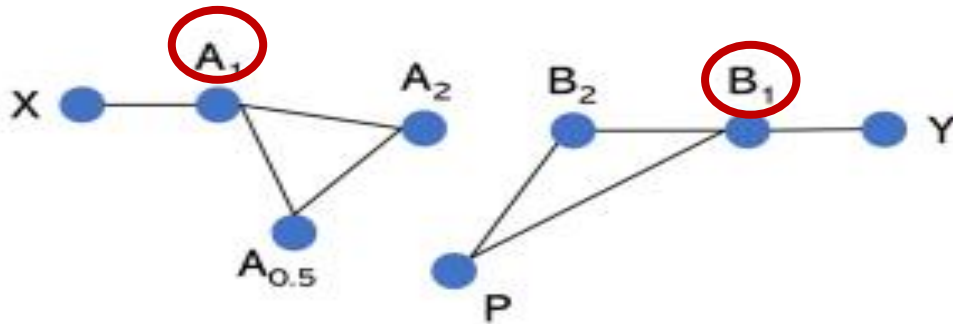


ILLUSTRATION

Studies of A

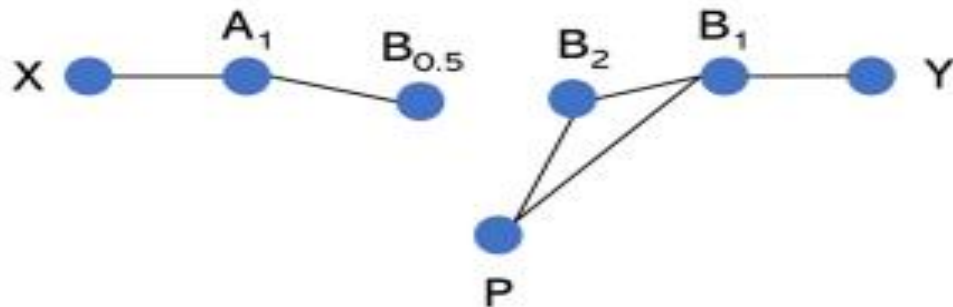
Studies of B

C



- A_1 and B_1 are disconnected.
- In figure C, A and B are disconnected due to **absence of common comparator**.
- In figure D, A and B are disconnected due to **comparison with unlicensed dose ($B_{0.5}$)**

D



Treatments are defined by agent,
(A, B, X, Y)

Dose 1 = licensed dose

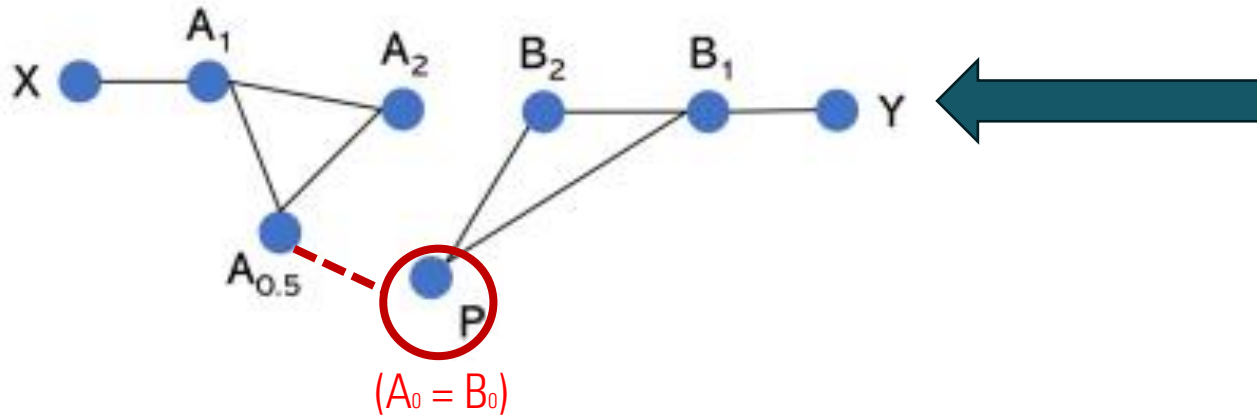
Dose 0.5 = $\frac{1}{2}$ of licensed dose



APPLYING MBNMA



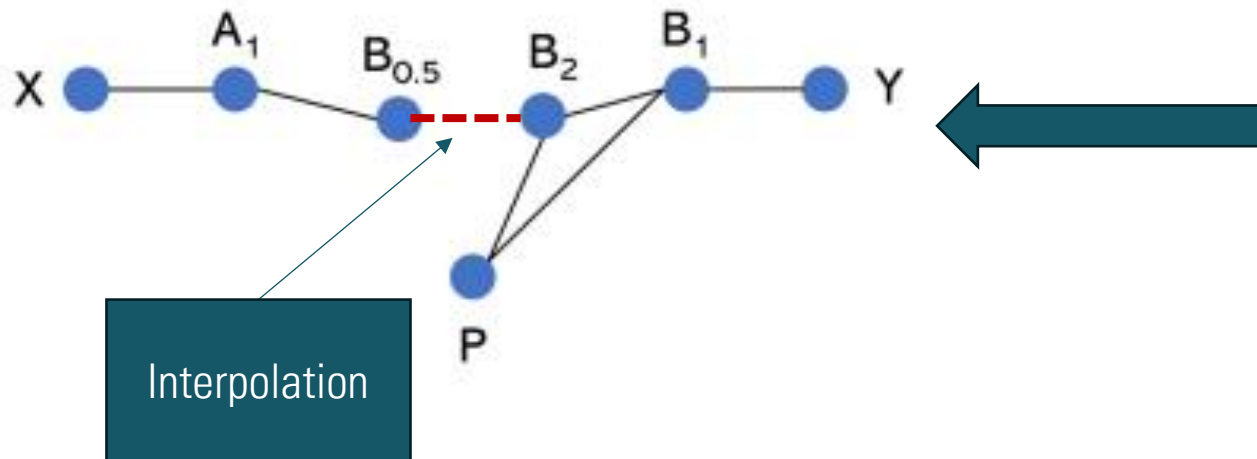
C



1. Use MBNMA modeling to connect the network by estimating **A placebo response of agents.**

Placebo response (p) = Dose 0 of each agent
($A_0 = B_0$)

D



2. Connects the different dose of treatment B (e.g $B_{0.5}$) **to other doses** of B by **interpolation.**

AIM OF STUDY

- To illustrate the potential of dose-response MBNMA to connect and strengthen evidence networks in a range of different scenarios.

1. Describe the MBNMA method

2. Introduce a network of triptans for migraine relief (data set)

3. Manipulate the data set to obtain a set of scenario networks with different features to illustrate the performance of the MBNMA method

4. Present and compare results from MBNMA and NMA in each scenario.



METHODS

1. THE STANDARD NMA METHOD

- Study-specific relative treatment effect ($\delta_{i,k}$) is assumed to follow a **normal distribution** around the **average (mean) treatment effect** for that comparison.
- This **mean treatment effect** reflects the **difference between the treatment ($t_{i,k}$)** used in arm k and the **reference treatment ($t_{i,1}$)** used in control arm (1) of each study.
- The **between-study variance (τ^2)** represents how much treatment effects vary across studies.

$$\delta_{i,k} \sim N(\underbrace{d_{t_{i,k}} - d_{t_{i,1}}}_{\text{Mean treatment effect } (t_{i,k}) \text{ vs the network reference treatment}}, \tau^2)$$

Mean treatment effect
($t_{i,k}$) vs the network
reference treatment

2. *THE DOSE-RESPONSE MBNMA METHOD*

- The dose-response MBNMA model extends the standard NMA model by incorporating a **dose-response relationship**.
- It defines the treatment in arm k of study i as a **specific dose ($x_{i,k}$)** of a **specific agent ($a_{i,k}$)**.

$$\delta_{i,k} \sim N(\underbrace{f(x_{i,k}, a_{i,k})}_{\text{Dose-response function for specific dose } (x_{i,k}) \text{ of a specific agent } (a_{i,k}) \text{ in arm } K} - \underbrace{f(x_{i,1}, a_{i,1})}_{\text{Dose-response function for specific dose } (x_{i,k}) \text{ of a specific agent } (a_{i,k}) \text{ in control arm of study } i}, \tau^2)$$

Dose-response function for specific
dose ($x_{i,k}$) of a specific agent ($a_{i,k}$).
In arm K

Dose-response function for specific
dose ($x_{i,k}$) of a specific agent ($a_{i,k}$).
In control arm of study i

DOSE-RESPONSE FUNCTION

- Depends on the number of doses of an agent included in RCTs in the network.

1. Exponential model function

- In this model, a **single** dose-response **parameter** is estimated for each agent.
- Studies with >2 doses (one of which could be placebo) of each agent are required to estimate **rate parameter** (i.e How fast the effect increase or decrease with dose)

$$f(x_{i,k}, a_{i,k}) = E_{0,i} + \underbrace{\beta_{a_{i,k}}}_{\text{The rate parameter agent in arm (k) of study i}} (1 - \underbrace{e^{-x_{i,k}}}_{\text{Exponential term}})$$

The rate parameter
agent in arm (k) of study
i

Exponential term

DOSE-RESPONSE FUNCTION

2. Emax function

- Studies with at least 3 doses of a specific agent are required.
- In this model, **2** dose-response **parameters** ($E_{\max}$ and ED_{50}) are estimated for each agent.
- The $E_{\max}$ and ED_{50} parameters may be correlated.
- This correlation is estimated by specifying a bivariate normal distribution with a Wishart prior on the covariance matrix.

$$f(x_{i,k}, a_{i,k}) = E_{0,i} + \frac{\overbrace{E_{\max, a_{i,k}} x_{i,k}}^{\text{Maximum achievable effect of specific agent}}}{\underbrace{ED_{50, a_{i,k}} + x_{i,k}}_{\text{Half-maximal effective dose}}}$$

IMPLEMENTATION

- Multiple datasets were created according to scenario.
- Each data set was analyzed where possible using **standard NMA** and **dose-response MBNMA**.
- **Common (Fixed)** and **random effects** models were compared for each model (NMA and MBNMA).
- Relative efficacy was presented in **posterior medians** and **95% credible intervals** (95% CrIs).
- e.g MBNMA with common effect vs MBNMA with random effect

IMPLEMENTATION

- **Model selection strategy**

1. Deviance information criterion (**DIC**) (defined as sum of the effective number of parameters added to the residual deviance) was used to **compare models**

- **Lowest DIC = Best model**

- Models with DIC within 3 points of **Best model** were identified, of these models, the simplest was preferred.

NMA or MBNMA Models with :	Preferred models (simplest model)
Fixed effect or Random effect	Fixed effect
Exponential dose-response or Emax dose-response function	exponential dose-response

- MBNMAdose version 0.2.727 package in R version 3.6.1 was used

INTRODUCING THE DATASET

- A data set of published RCTs for the efficacy of triptans in migraine relief.
- 70 studies
- 22 treatments
- 7 agents + placebo
- Doses are standardized to multiples of each agent's "common" dose.

Meta-Analysis > Cephalalgia. 2014 Apr;34(4):258-67. doi: 10.1177/0333102413508661.

Epub 2013 Oct 9.

Comparative efficacy of triptans for the abortive treatment of migraine: a multiple treatment comparison meta-analysis

Kristian Thorlund¹, Edward J Mills, Ping Wu, Elodie Ramos, Anjan Chatterjee, Eric Druyts, Peter J Goadsby



-
- Placebo
 - Eletriptan
 - Sumatriptan
 - Frovatriptan
 - Almotriptan
 - Zolmitriptan
 - Naratriptan
 - Rizatriptan



DATASET MANIPULATION

- From the complete data set, manipulated data sets were generated by removing **specific treatments** and **studies** to represent **several scenarios** that might be **found in practice**.
- Then performance of NMA and MBNMA methods in each scenario were compared.
- If only a **single arm remained** in a study after excluding another treatment arm, that study was excluded in the analysis.

SCENARIOS

1. DATA SET MANIPULATION
2. RESULTS FOR THAT SCENARIO

SCENARIO 1

Connected networks

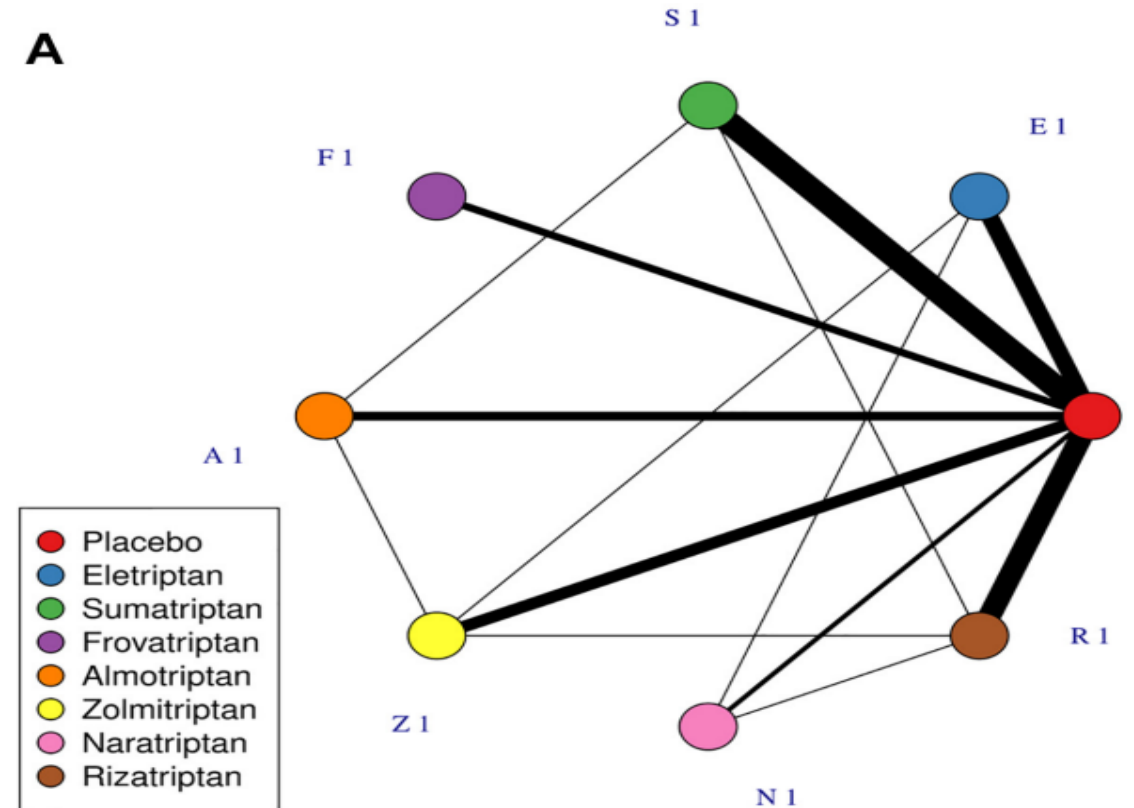
SCENARIO 1A

common

- The network is **connected** using **common** (licensed) dose per agent.
- This scenario is similar to data sets found in most studies, **whereby only licensed doses of each agent are of interest.**

- Manipulated data set included 59 RCTs
- Only a **single common dose** of each treatment and placebo is included.
- 7 treatments + placebo

A



SCENARIO 1A RESULTS

- Model fit

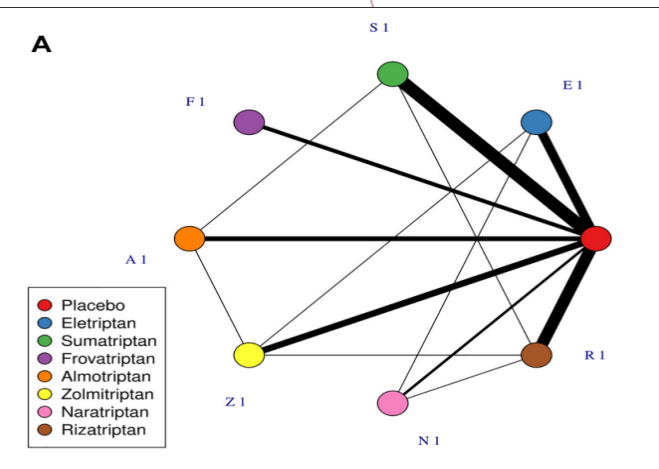


Table 1 Model Fit Statistics for All Models Investigated in Scenario 1A and 1B Data Sets

Data Set	No. of Data Points	Residual Deviance	DIC ^a	pD ^b	Model	Dose-Response Function	Treatment Effects	Between-Study SD (95% CrI)
Scenario 1A	122	202.3	66.6	268.9	NMA	NA	Common	NA
Scenario 1A	122	124.0	96.3	220.3	NMA	NA	Random	0.36 (0.25, 0.50)
Scenario 1A	122	201.7	66.1	267.8	MBNMA	Exponential	Common	NA
Scenario 1A	122	124.0	96.2	220.2	MBNMA	Exponential	Random	0.36 (0.25, 0.50)
Scenario 1A	122	NC	NC	NC	MBNMA	Emax	Common	NA
Scenario 1A	122	NC	NC	NC	MBNMA	Emax	Random	NC
Scenario 1B	182	269.0	93.3	362.3	NMA	NA	Common	NA
Scenario 1B	182	190.6	131.6	322.2	NMA	NA	Random	0.27 (0.18, 0.37)
Scenario 1B	182	296.5	77.1	373.6	MBNMA	Exponential	Common	NA
Scenario 1B	182	189.4	125.1	314.5	MBNMA	Exponential	Random	0.28 (0.20, 0.37)
Scenario 1B	182	266.8	80.9	347.7	MBNMA	Emax	Common	NA
Scenario 1B	182	191.7	121.6	121.6	MBNMA	Emax	Random	0.24 (0.16, 0.34)

^aDIC: deviance information criterion = pD + residual deviance.

^bpD: The effective number of parameters calculated using the Kullback-Leibler divergence³⁰ for model-based network meta-analysis (MBNMA) and the plugin method²⁹ for NMA.

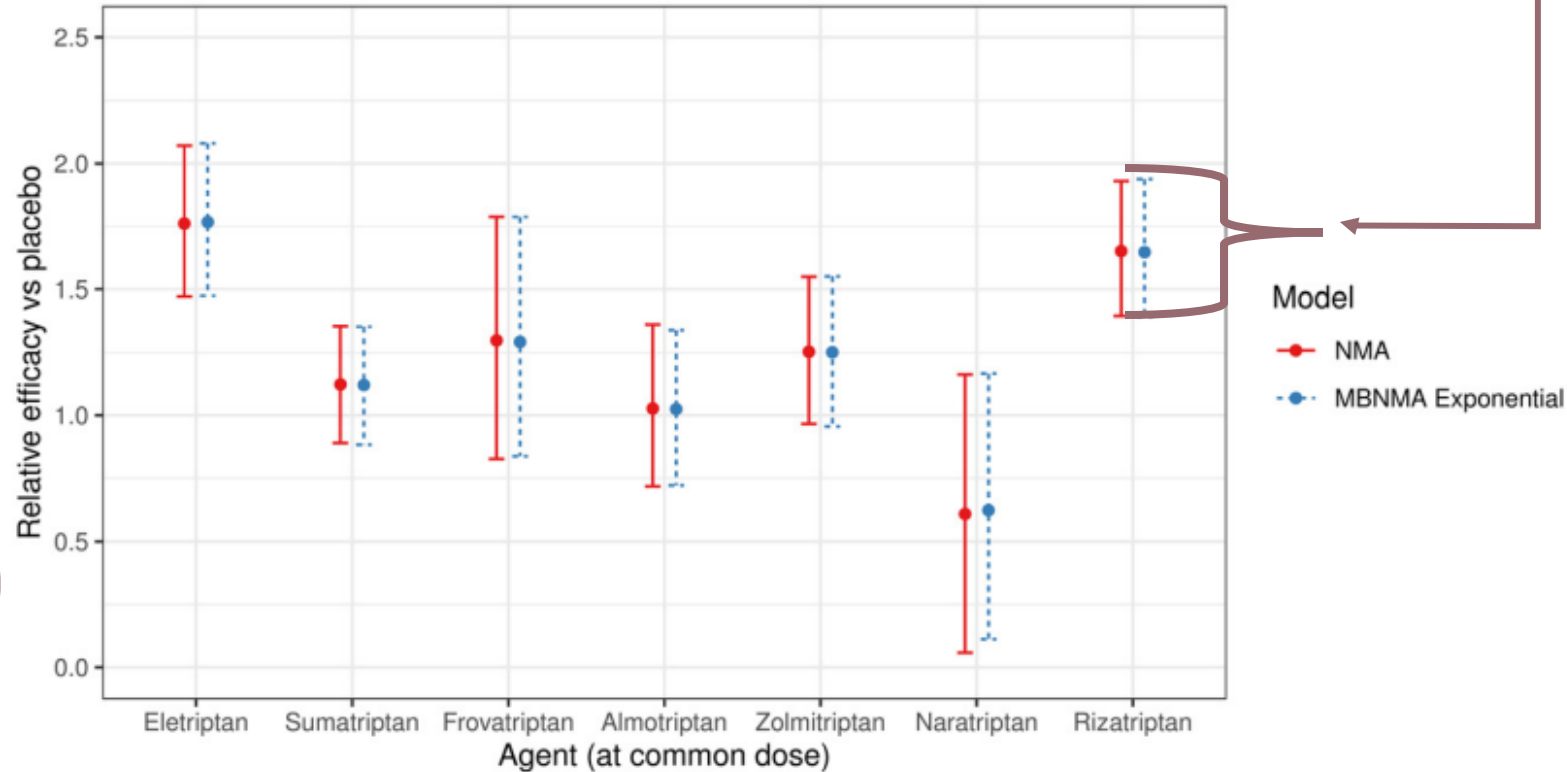
NC, Markov chain Monte Carlo chains did not converge; model was not identifiable.

NA: not applicable

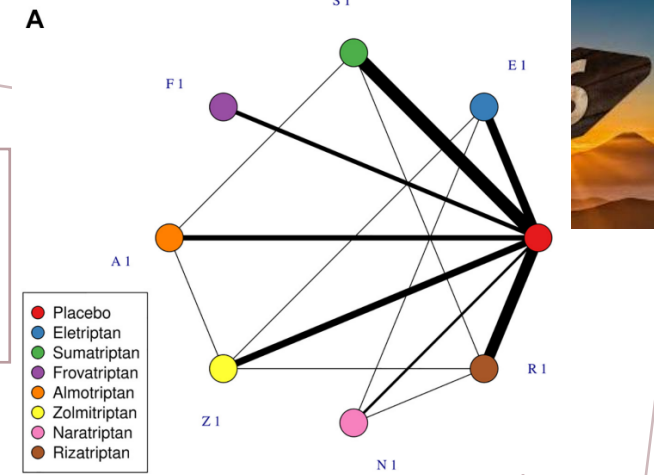
- The exponential MBNMA model and NMA with random effect was chosen.
- Model performance of NMA (DIC=96.3) and MBNMA (DIC= 96.2) is similar.

SCENARIO 1A RESULTS

- Relative effect



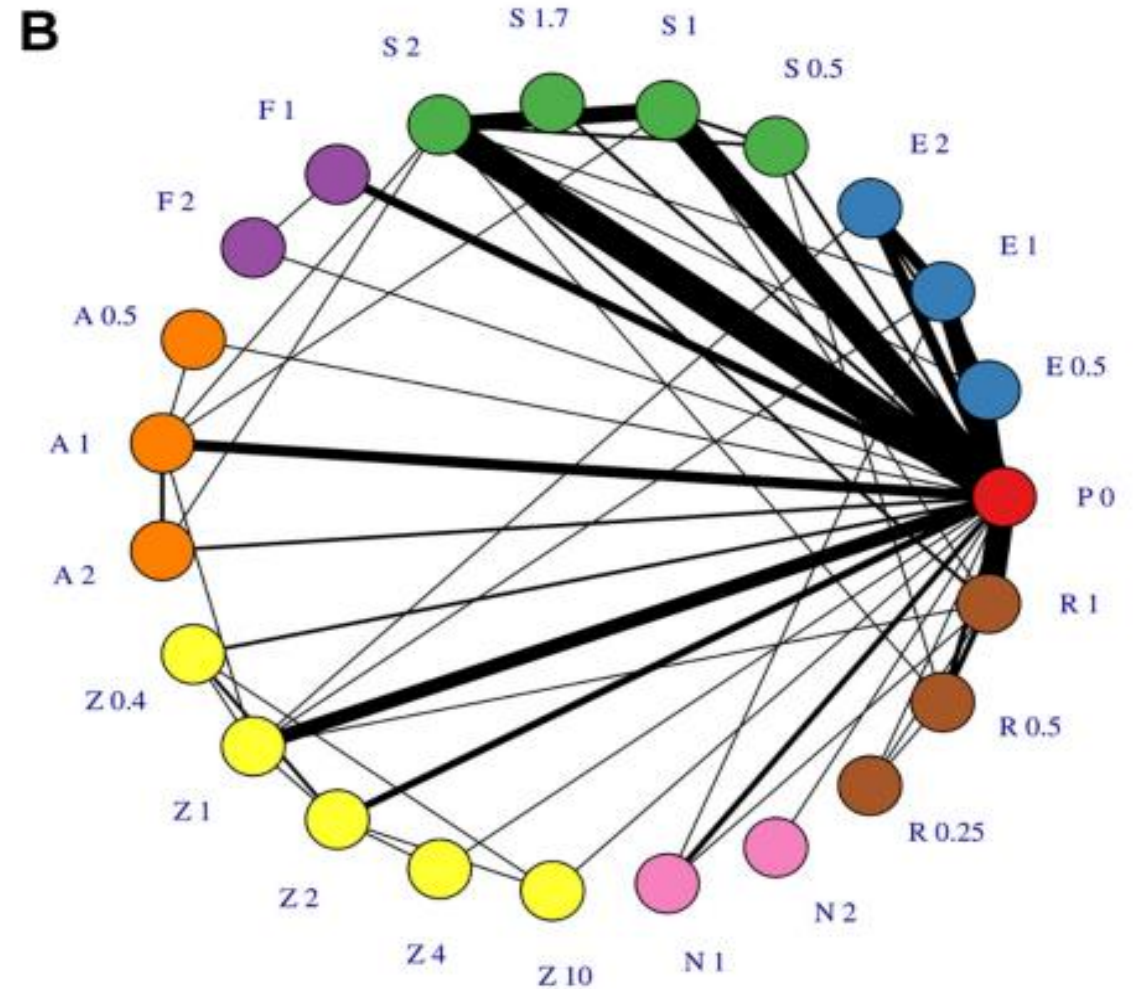
Relative effects from selected NMA and MBNMA models were very similar.



Because of the **lack of dose response information**,
There was no gain in **precision** of the estimates in the MBNMA model vs the NMA model.

SCENARIO 1B

- Dataset was generated in such a way that a network was **connected** using evidence of **all available doses of each agent** and placebo.
- 70 studies,
- 22 treatments, 7 agents, and a placebo



SCENARIO 1B RESULTS

- Model fit

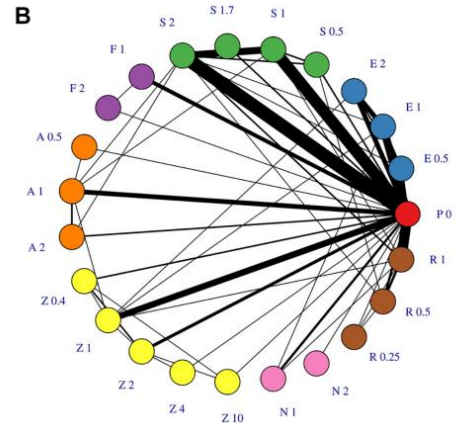


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Scenario 1A	122	201.7	66.1	267.8	MBNMA	Exponential	Common	NA
Scenario 1A	122	124.0	96.2	220.2	MBNMA	Exponential	Random	0.36 (0.25, 0.50)
Scenario 1A	122	NC	NC	NC	MBNMA	E _{max}	Common	NA
Scenario 1A	122	NC	NC	NC	MBNMA	E _{max}	Random	NC
Scenario 1B	182	269.0	93.3	362.3	NMA	NA	Common	NA
Scenario 1B	182	190.6	131.6	322.2	NMA	NA	Random	0.27 (0.18, 0.37)
Scenario 1B	182	296.5	77.1	373.6	MBNMA	Exponential	Common	NA
Scenario 1B	182	189.4	125.1	314.5	MBNMA	Exponential	Random	0.28 (0.20, 0.37)
Scenario 1B	182	266.8	80.9	347.7	MBNMA	E _{max}	Common	NA
Scenario 1B	182	191.7	121.6	121.6	MBNMA	E _{max}	Random	0.24 (0.16, 0.34)

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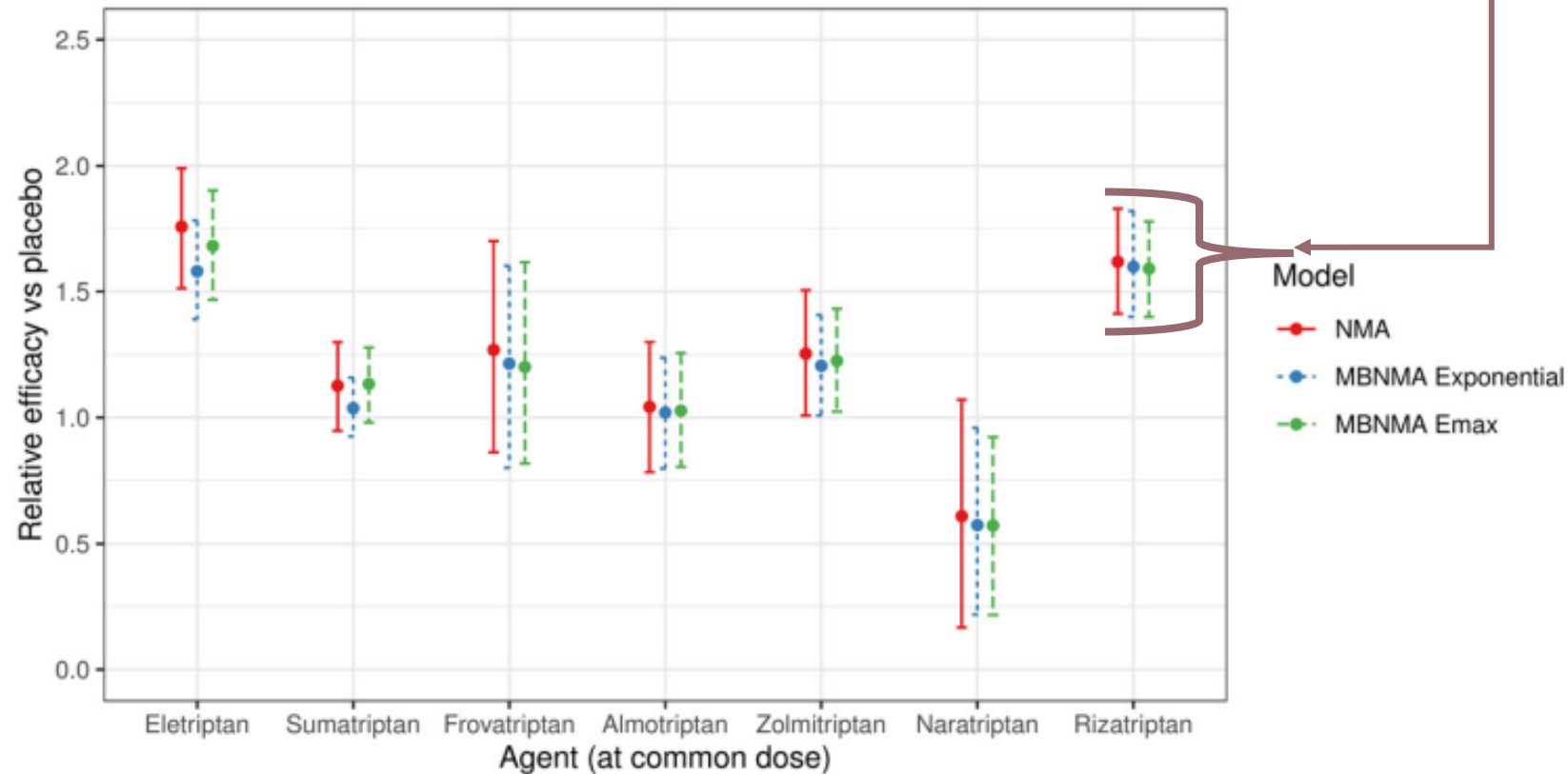
NC, Markov chain Monte Carlo chains did not converge; model was not identifiable.

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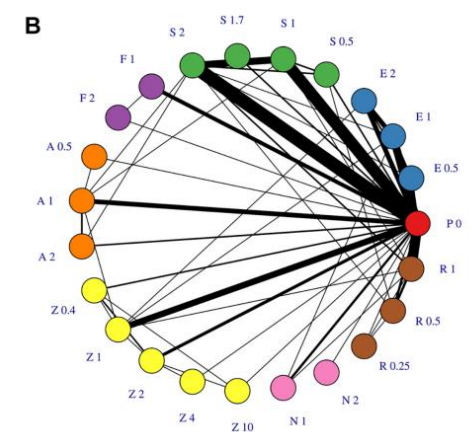
- Random effects models were selected for the NMA and MBNMA.
- An E_{max} dose response function was selected for the MBNMA model (DIC =121.6)

SCENARIO 1B RESULTS

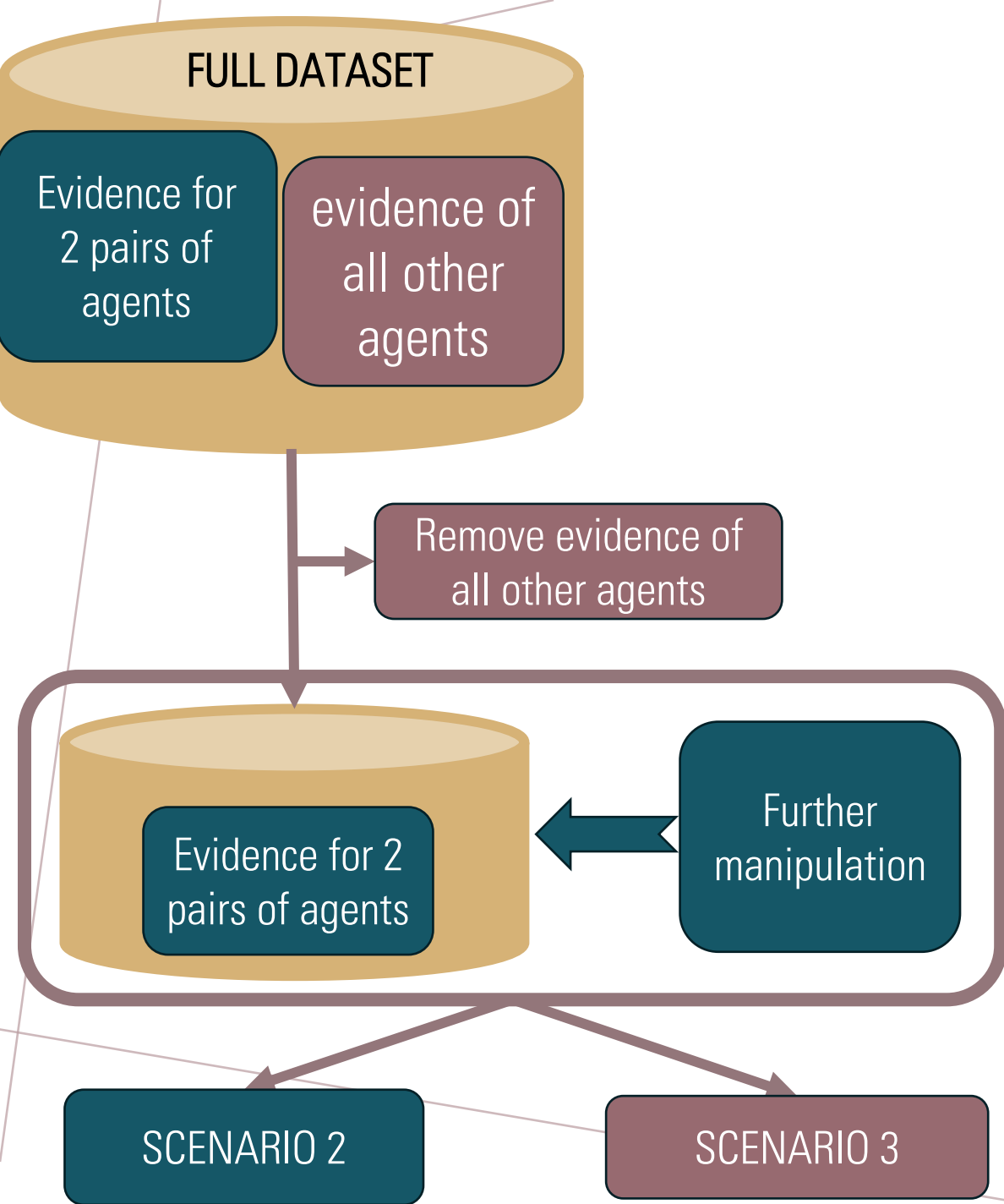
- Relative effect



MBNMA estimates were **more precise** than NMA estimates



- Additional information gained from modeling the dose-response relationship led to **increased precision** in MBNMA estimates vs NMA estimates.



SCENARIO 2 AND 3

- Disconnected networks
- The objective was to compare 2 treatments of interest (agents of interest at the common dose)
- The datasets were manipulated to obtain **disconnected networks for scenarios.**

SCENARIO 2 AND 3

Step 1

- Fit the MBNMA models to disconnected networks using method described in previous study
- Calculate relative effects

Step 2

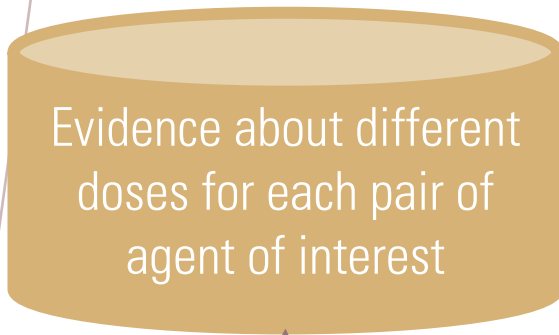
- Add data to create “augmented datasets” to connect the network
- Calculate relative effects

Step 3

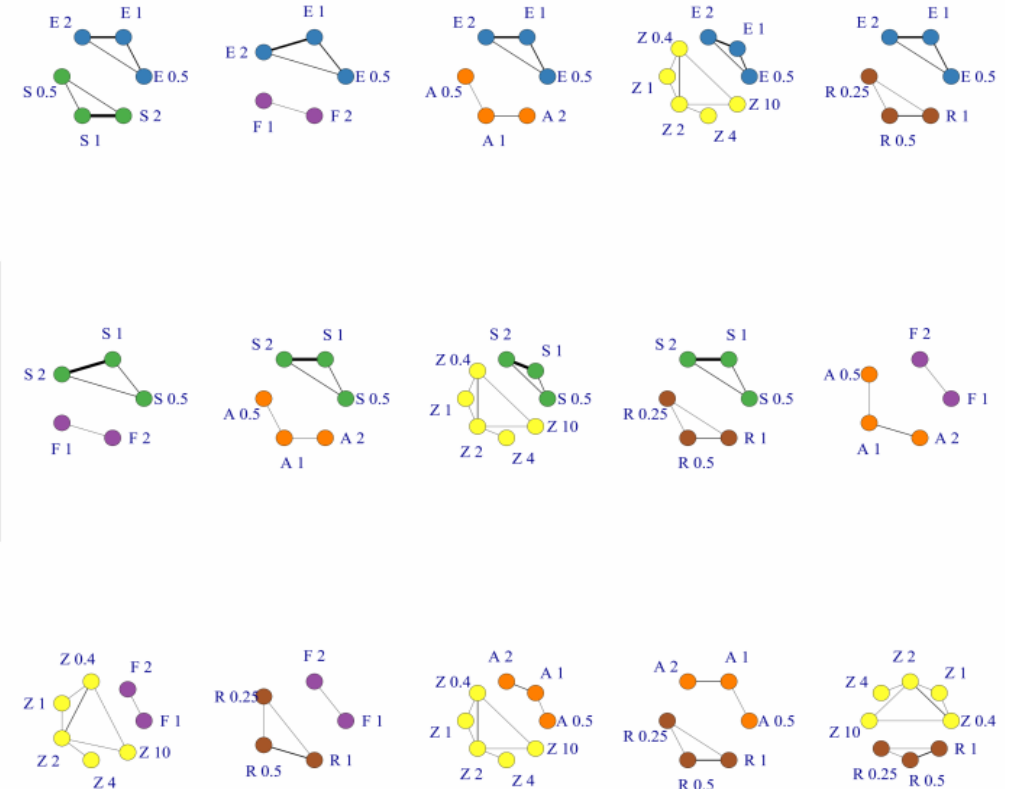
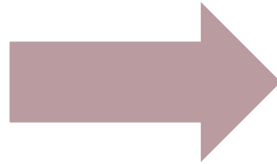
- Compare the relative effects estimated between 2 datasets and assess level of agreement

SCENARIO 2

- Created situation whereby the network is **disconnected** due to absence of common comparator (e.g placebo).
- There is **evidence on different doses** for an agent of interest but there is no common comparator.
- **All placebo arms** for each pair of agents comparison were removed



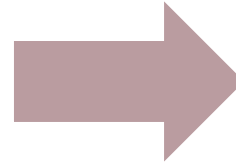
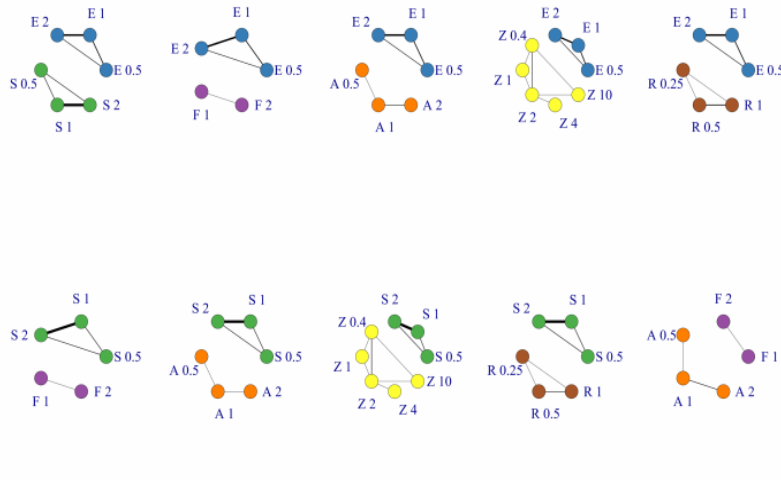
Remove placebo arm



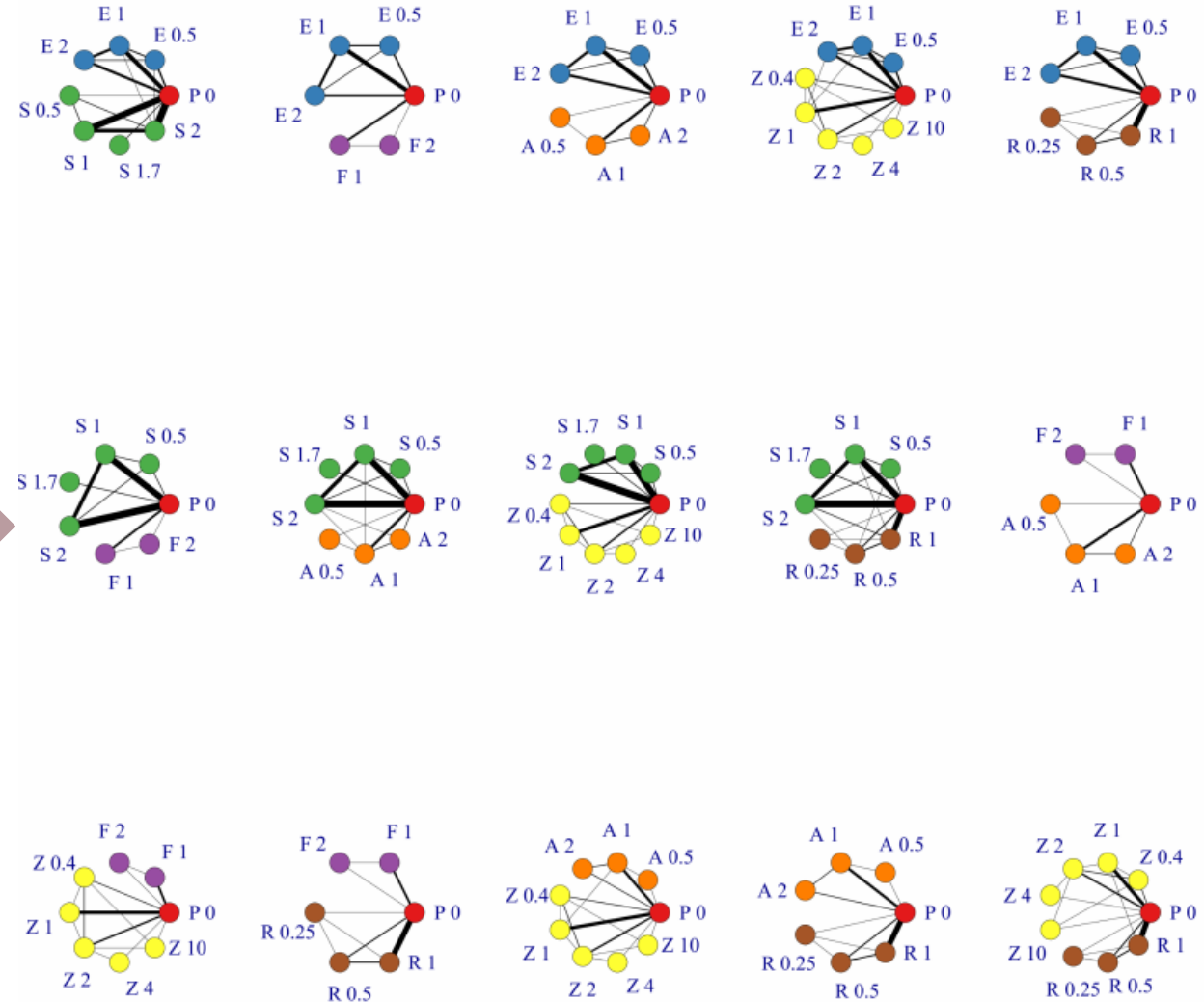
SCENARIO 2

- Generation of augmented datasets
- BY including comparisons between **any doses** of the included agents **versus placebo**

Disconnected networks



Connected networks by augmentation



SCENARIO 2 RESULTS



- NMA models could not be estimated because of the networks being disconnected.
- In all **disconnected data sets**,
an exponential dose response MBNMA was selected with common treatment effects
- In **Augmented data sets**,
- For **MBNMA** models, an **E_{max} dose-response** function was selected for **12 of 15** data sets.
- **Random treatment effects** were selected over common effects in **12 of 15** data sets for both NMA and MBNMA models.

SCENARIO 2 RESULTS

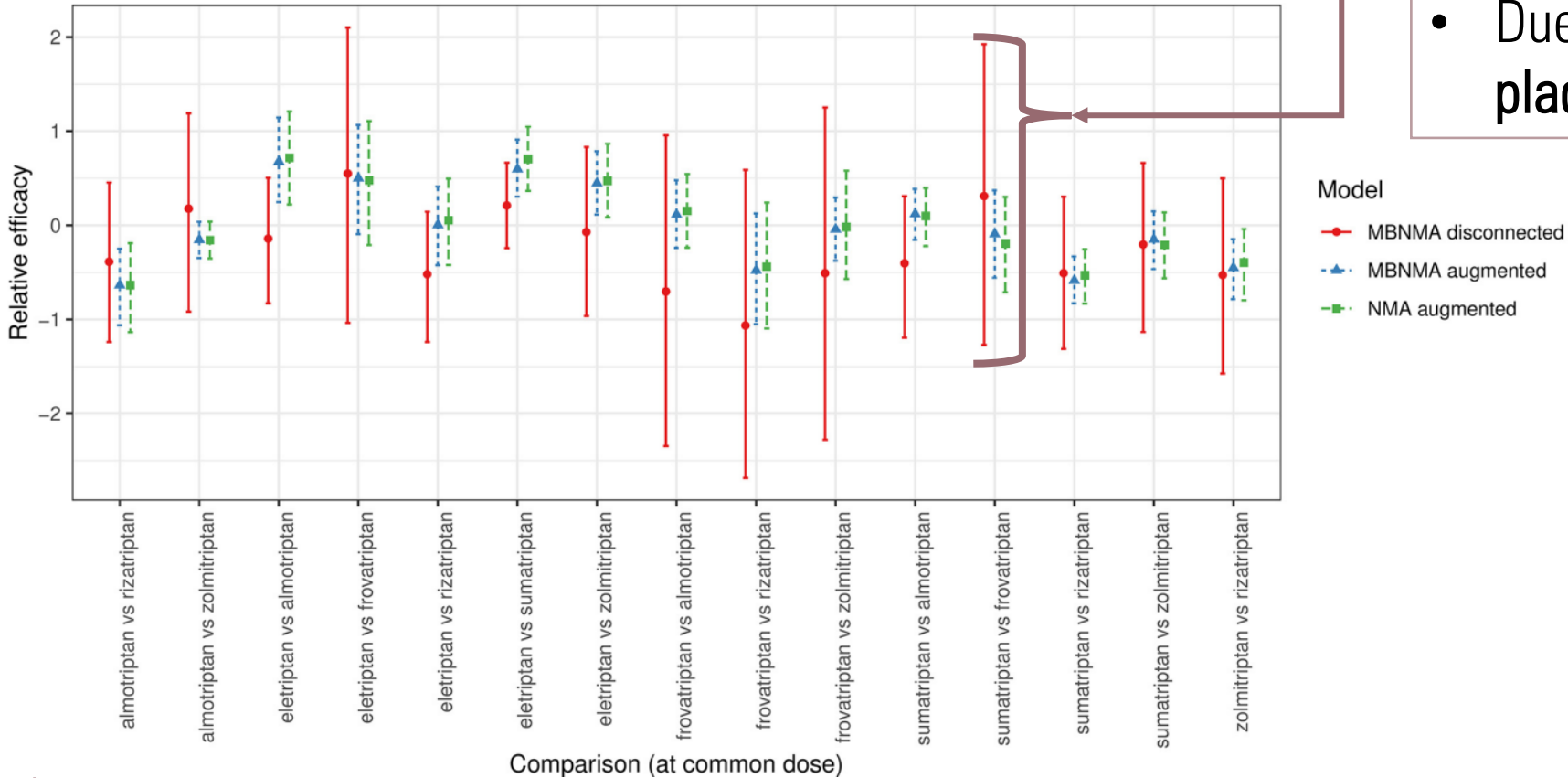


Table 2 Model Fit Statistics for Selected Models in Each Data Set Analyzed in Scenario 2

Data Set Number	Data Set	Agent 1	Agent 2	No. of Data Points	Residual Deviance	DIC ^a	AIC ^b	Model	Dose-Response Function	Treatment Effects	Between-Study SD
1	Initial	Almotriptan	Rizatriptan	13	12.0	20.0	8.0	MBNMA	Exponential	Common	NA
1	Augmented	Almotriptan	Rizatriptan	45	48.9	81.5	32.6	MBNMA	Exponential	Random	0.27 (0.09–0.5)
1	Augmented	Almotriptan	Rizatriptan	45	48.1	83.3	35.3	NMA	NA	Random	0.32 (0.12–0.59)
2	Initial	Almotriptan	Zolmitriptan	14	11.0	19.2	8.2	MBNMA	Exponential	Common	NA
2	Augmented	Almotriptan	Zolmitriptan	44	42.1	63.0	21.0	MBNMA	E _{max}	Common	NA
2	Augmented	Almotriptan	Zolmitriptan	44	45.3	71.6	26.3	NMA	NA	Common	NA
3	Initial	Eletriptan	Almotriptan	22	24.0	36.3	12.3	MBNMA	Exponential	Common	NA
3	Augmented	Eletriptan	Almotriptan	46	48.1	81.7	33.6	MBNMA	E _{max}	Random	0.3 (0.14–0.5)
3	Augmented	Eletriptan	Almotriptan	46	48.3	84.5	36.3	NMA	NA	Random	0.34 (0.16–0.58)
4	Initial	Eletriptan	Frovatriptan	18	21.6	31.9	10.2	MBNMA	Exponential	Common	NA
4	Augmented	Eletriptan	Frovatriptan	42	42.1	76.0	34.0	MBNMA	E _{max}	Random	0.4 (0.23–0.67)
4	Augmented	Eletriptan	Frovatriptan	42	42.8	77.0	34.2	NMA	NA	Random	0.43 (0.23–0.71)
5	Initial	Eletriptan	Rizatriptan	23	27.9	39.9	12.1	MBNMA	Exponential	Common	NA
5	Augmented	Eletriptan	Rizatriptan	61	63.1	110.2	47.2	MBNMA	E _{max}	Random	0.38 (0.23–0.57)
5	Augmented	Eletriptan	Rizatriptan	61	63.9	112.0	48.1	NMA	NA	Random	0.4 (0.24–0.63)

- In all disconnected (initial) data sets, an exponential dose response MBNMA was selected with common treatment effects.

SCENARIO 2 RESULTS

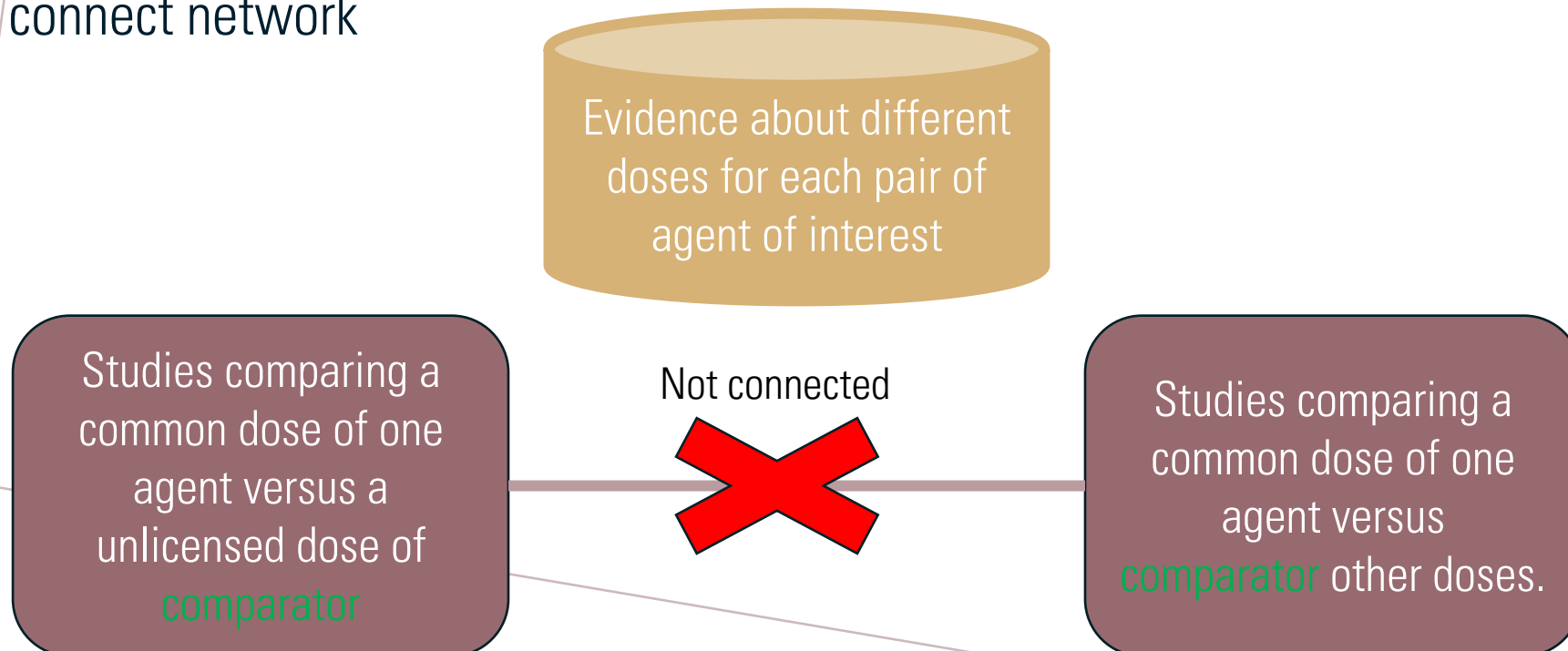


- High uncertainty in relative effects from disconnected MBNMA models
- Due to **sparse data** and **lack of placebo evidence** at lower doses

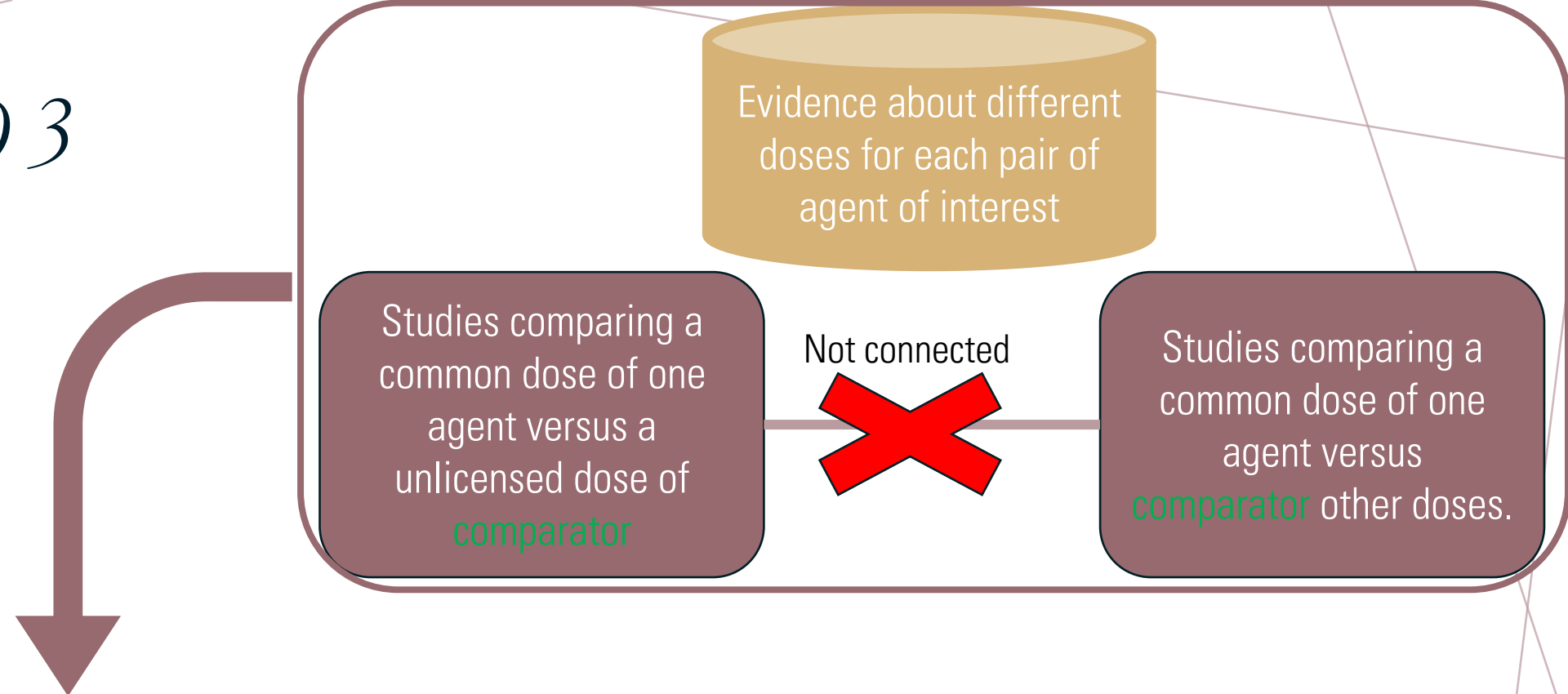
- **Augmenting data** with placebo arms improved network connectivity
- **MBNMA and NMA estimates** became very similar after augmentation.
- **MBNMA** showed slightly higher precision with **narrower 95% CrIs**

SCENARIO 3

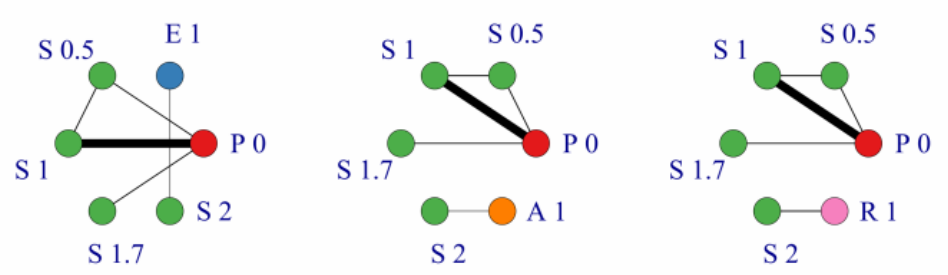
- Created situation whereby the network is **disconnected** due to comparison with a dose that has not been evaluated in other trials.
- There is **evidence on** the treatment of interest been investigated in studies only comparing it with unlicensed dose of a comparator.
- The augmented data sets that include comparisons between all doses of both agents were generated to connect network



SCENARIO 3



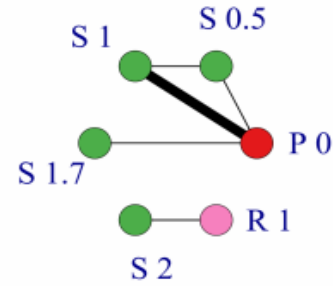
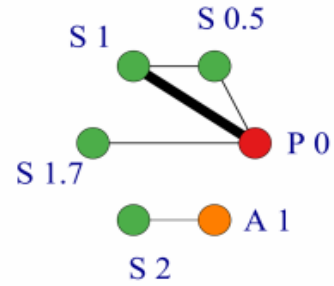
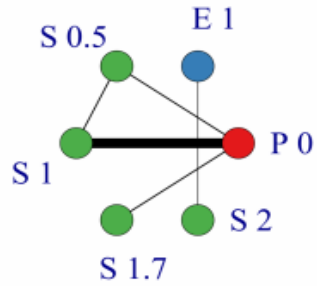
- Placebo
- Eletriptan
- Sumatriptan
- Frovatriptan
- Almotriptan
- Zolmitriptan
- Naratriptan
- Rizatriptan



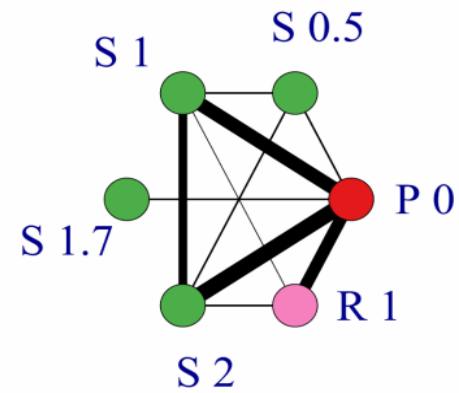
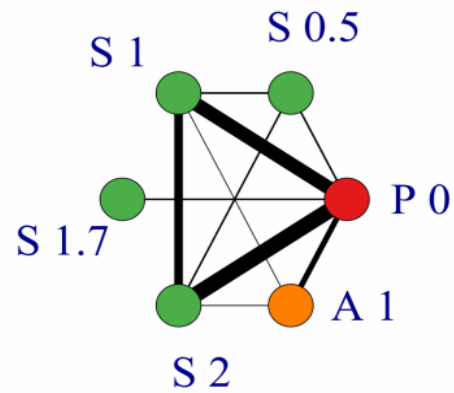
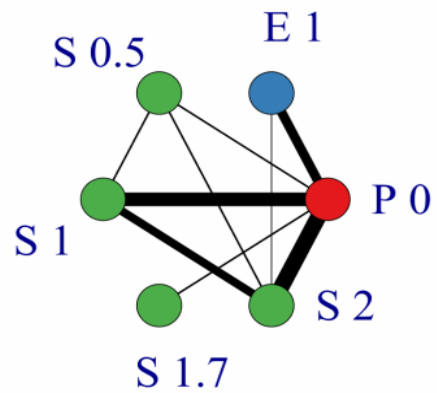
Disconnected network

SCENARIO 3

- Placebo
- Eletriptan
- Sumatriptan
- Frovatriptan
- Almotriptan
- Zolmitriptan
- Naratriptan
- Rizatriptan



Augmented network



SCENARIO 3 RESULTS

Table 3 Model Fit Statistics for Selected MBNMA and NMA Models in Each Data Set Analyzed in Scenario 3

Dataset Number	Data Set	Agent 1	Agent 2	No. of Data Points	Residual Deviance	DIC ^a	pD ^b	Model	Dose-Response Function	Treatment Effects	Between-Study SD
1	Initial	Almotriptan	Sumatriptan	38	37.5	66.6	29.1	MBNMA	Exponential	Random	0.30 (0.10–0.54)
1	Augmented	Almotriptan	Sumatriptan	74	74.3	127.5	53.3	MBNMA	Exponential	Random	0.28 (0.16–0.44)
1	Augmented	Almotriptan	Sumatriptan	74	75.3	128.6	53.3	NMA	NA	Random	0.27 (0.12–0.42)
2	Initial	Eletriptan	Sumatriptan	38	37.2	66.8	29.6	MBNMA	Exponential	Random	0.29 (0.11–0.54)
2	Augmented	Eletriptan	Sumatriptan	80	81.1	141.0	59.8	MBNMA	Exponential	Random	0.35 (0.22–0.52)
2	Augmented	Eletriptan	Sumatriptan	80	81.0	142.5	61.6	NMA	NA	Random	0.36 (0.22–0.53)
3	Initial	Rizatriptan	Sumatriptan	40	38.6	69.2	30.6	MBNMA	Exponential	Random	0.28 (0.11–0.53)
3	Augmented	Rizatriptan	Sumatriptan	87	89.0	152.9	63.9	MBNMA	Exponential	Random	0.32 (0.21–0.48)
3	Augmented	Rizatriptan	Sumatriptan	87	89.5	154.1	64.6	NMA	NA	Random	0.32 (0.20–0.47)

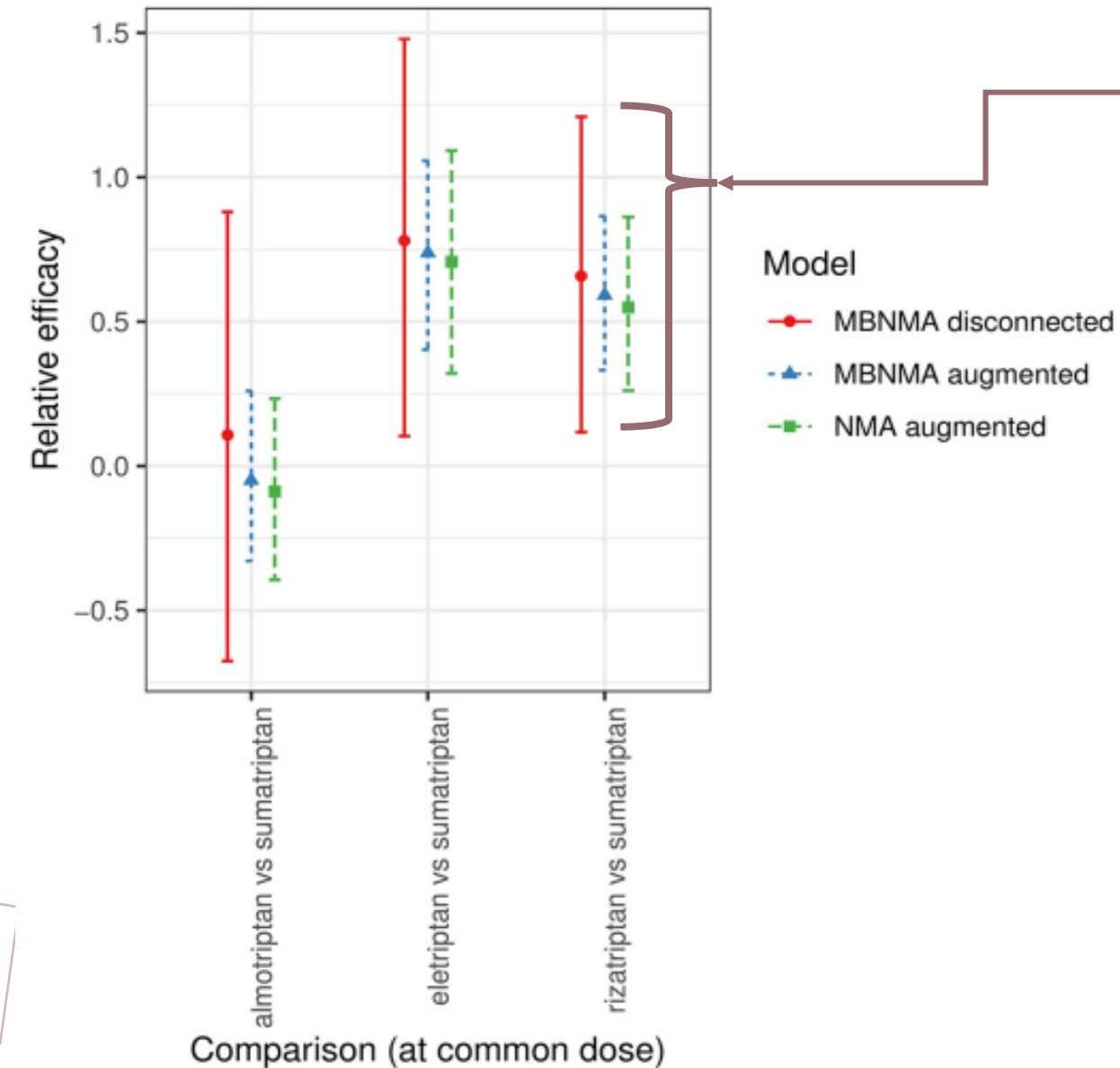
^aDIC: deviance information criterion = pD + residual deviance.

^bpD: The effective number of parameters calculated using the Kullback-Leibler divergence³⁰ for model-based network meta-analysis (MBNMA) and the plugin method²⁹ for NMA.

NA: not applicable

- Exponential MBNMA models with random treatment effects were selected in disconnected networks (Initial) and augmented
- Random effects models were selected in all data sets for NMA models

SCENARIO 3 RESULTS



- Still High uncertainty in disconnected MBNMA models
- Estimates in augmented data sets were **within the 95% CrIs** of those from MBNMAs in the disconnected data sets suggesting that **results were in agreement**

- For Augmenting data
- MBNMA and NMA estimates were very similar
- Higher precision in MBNMA estimates

DISCUSSION

- The study illustrate scenarios in which dose response MBNMA can be used to strengthen the NMA method by either increasing precision or connecting the disconnected networks.
- This can be done by adding evidence of unlicensed doses and modeling a functional dose repose relationship.
- Connection can be done by linking different doses of the same agent along the dose response curve
- Or link different agents by extrapolating a placebo response.
- In HTAs with connected networks, whereby multiple doses are of interest, using MBNMA can be of benefit,  precision

DISCUSSION

- In disconnected networks (scenarios 2 and 3), MBNMA estimates were consistent with NMA estimates from augmented datasets.
- Although MBMNA could be estimated In situation where there is no common comparators between 2 agents (scenario 2), a complex dose-response function could not be fitted due to lack of information of different dose of each agent.
- In scenario 3 (one of the agents of interest were compared to the unlicensed dose of another agent) MBNMA was able to link the agents at licensed dose.
- In this scenario, estimates from the disconnected and augmented data sets agreed, could be due to availability of evidence of different doses of agents connected via dose-response relationship.

DISCUSSION

- MBNMA approach uses RCTs only and does not violate the randomization in RCTs thus provide unbiased estimates.
- Can be fitted using aggregate data only, no need for individual patient data

Provided that Important assumptions of:

- Consistency assumption
- dose-response function correct specification are met

OTHER METHODS FOR DISCONNECTED NETWORKS

- Model-based meta-analysis (MBMA)
- Predict effect of reference treatment by random effects
- Population adjustment methods (e.g matched adjusted indirect comparisons or simulated treatment comparisons)
- Component network meta-analysis
- A joint analysis using multivariate NMA
- Time-course MBNMA
- Assuming a common or exchangeable effect among similar treatments

LIMITATIONS

- Dose-response MBNMA is sensitive to misspecification of the dose response function.
- Complex functions like Emax model require data on multiple doses of different agents to be able to estimate them.
- In case there is only one dose + placebo OR 2 doses without placebo for each agent, only simple functions like linear or exponential can be fitted.
- Model fit statistics cannot help distinguish between simple dose response function models.
- Simulation studies to explore the performance of MBNMA models for different evidence structures would be a useful area for further work.

CONCLUSIONS

- **NMA** requires connected treatment networks
- **MBNMA** reconnects disconnected networks using **dose–response relationships** when evidence on multiple doses of agents is available.
- In augmented data sets, the MBNMA and NMA estimates were in agreement.
- MBNMA adds an extra assumption: **the dose–response relationship is correctly specified** (can be checked via model fit)
- MBNMA can use **aggregate data** and often provides **greater precision** than NMA when multiple doses exist
- Requires **data on multiple doses** for each treatment to work effectively





THANK YOU