

Article



Using multiple genetic variants as instrumental variables for modifiable risk factors

Statistical Methods in Medical Research 21(3) 223–242 © The Author(s) 2011 Reprints and permissions: sagepub.co.uk/journalsPermissions.nav DOI: 10.1177/0962280210394459 smm.sagepub.com



Tom M Palmer, Debbie A Lawlor, Soger M Harbord, Nuala A Sheehan, Jon H Tobias, Nicholas J Timpson, George Davey Smith and Jonathan AC Sterne

Abstract

Mendelian randomisation analyses use genetic variants as instrumental variables (IVs) to estimate causal effects of modifiable risk factors on disease outcomes. Genetic variants typically explain a small proportion of the variability in risk factors; hence Mendelian randomisation analyses can require large sample sizes. However, an increasing number of genetic variants have been found to be robustly associated with disease-related outcomes in genome-wide association studies. Use of multiple instruments can improve the precision of IV estimates, and also permit examination of underlying IV assumptions. We discuss the use of multiple genetic variants in Mendelian randomisation analyses with continuous outcome variables where all relationships are assumed to be linear. We describe possible violations of IV assumptions, and how multiple instrument analyses can be used to identify them. We present an example using four adiposity-associated genetic variants as IVs for the causal effect of fat mass on bone density, using data on 5509 children enrolled in the ALSPAC birth cohort study. We also use simulation studies to examine the effect of different sets of IVs on precision and bias. When each instrument independently explains variability in the risk factor, use of multiple instruments increases the precision of IV estimates. However, inclusion of weak instruments could increase finite sample bias. Missing data on multiple genetic variants can diminish the available sample size, compared with single instrument analyses. In simulations with additive genotype-risk factor effects, IV estimates using a weighted allele score had similar properties to estimates using multiple instruments. Under the correct conditions, multiple instrument analyses are a promising approach for Mendelian randomisation studies. Further research is required into multiple imputation methods to address missing data issues in IV estimation.

Keywords

causal inference, econometrics, epidemiology, genetics, instrumental variables, Mendelian randomisation

Corresponding author:

Tom M Palmer, MRC Centre for Causal Analyses in Translational Epidemiology, Oakfield House, Oakfield Grove, Bristol, BS8 2BN, UK

Email: tom.palmer@bristol.ac.uk

¹MRC Centre for Causal Analyses in Translational Epidemiology, School of Social and Community Medicine, University of Bristol, Bristol, UK

²School of Social and Community Medicine, University of Bristol, Bristol, UK

³Departments of Health Sciences and Genetics, University of Leicester, Leicester, UK

⁴School of Clinical Sciences, University of Bristol, Bristol, UK

I Introduction

Mendelian randomisation analyses use genetic variants as instrumental variables (IVs) to make causal inferences about the effect of modifiable risk factors on health- and disease-related outcomes in the presence of unobserved confounding of the relationship of interest.^{1–5} Use of Mendelian randomisation is growing rapidly.^{4–7} However, using genetic variants as IVs poses statistical challenges.^{5,8–11} In particular, there is a need for large sample sizes because of the relatively small proportion of variation in risk factors typically explained by genetic variants.^{5,12,13}

Recent decreases in genotyping costs and increases in genome-wide association studies (GWAS), have facilitated discovery of a substantial number of genetic variants associated with risk factors and disease-related outcomes, such as adiposity^{14–16} and type 2 diabetes.^{17–27} Consideration of multiple instruments for Mendelian randomisation applications is therefore timely due to increasing availability of suitable variants. In this article we discuss the use of multiple genetic variants as IVs, both for increasing statistical precision and for testing underlying IV assumptions.

The structure of the article is as follows: we describe instrumental variable assumptions (Section 1.1) and introduce an illustrative Mendelian randomisation analysis and present separate IV estimates for four instruments (Section 2). We then discuss the use of multiple instruments to help address some of the genetic and statistical issues that can affect Mendelian randomisation analyses (Sections 3 and 4), including the results of simulation studies (Section 5). We return to the example and simulation to compare IV estimates using multiple instruments and allele scores (Section 6), assess the impact of missing data (Section 6.2) and discuss the implications of our findings (Section 7).

1.1 Instrumental variable assumptions

An IV (instrument) G is defined as a variable that satisfies the following assumptions:

- (1) G is associated with the risk factor (phenotype or intermediate variable) of interest X;
- (2) G is independent of the (unobserved) confounding factors U of the association between X and the outcome Y:
- (3) G is independent of outcome Y given X and U.

In the context of Mendelian randomisation, these assumptions can be expressed as: genotype is associated with the modifiable risk factor of interest (assumption 1); genotype is independent of unmeasured confounding factors that could bias conventional epidemiological associations between the risk factor and the outcome (assumption 2); genotype is related to the outcome only via its association with the risk factor (assumption 3). The second assumption can be justified through Mendel's laws when applied to independent heritable units.^{5,28}

If we further assume that intervention on the risk factor only affects the value of the risk factor, and hence affects the outcome only through this induced change in the risk factor, then the IV assumptions imply the 'exclusion restriction' 11,29 and its weaker form known as 'conditional mean independence' (used in structural mean models). This additional assumption allows causal inferences to be drawn from IV analyses.

2 Illustrative Mendelian randomisation analysis: single instrument estimates

Our example investigates the causal effect of fat mass on bone mineral density (BMD) using four genotypes known to be associated with adiposity from previous GWAS. A previous study found a

positive effect of fat mass on BMD using SNPs associated with the FTO and MC4R genes as IVs.³¹ The authors concluded that higher fat mass caused increased accrual of bone mass in childhood. We consider whether the IV estimates from the separate instruments are of similar magnitude; whether use of multiple instruments increases the precision of IV estimates; the use of allele scores as IVs; and the impact of missing data on IV estimates.

2.1 Data

Our example uses data from the Avon Longitudinal Study of Parents and Children (ALSPAC).³² ALSPAC is a longitudinal, population-based birth cohort study that recruited 14 541 pregnant women resident in Avon, UK, with expected dates of delivery 1 April 1991 to 31 December 1992 (http://www.alspac.bris.ac.uk).³² Out of this 13 988 live born infants survived to at least one year of age. Children eligible for inclusion in our analysis: (1) had DNA available for genotyping; (2) attended the research clinic at age 9 and (3) had complete data on height and dual energy X-ray densitometry (DXA) scan-determined total fat mass and total BMD.

2.2 Selection of genotypes

Eleven adiposity-related SNPs identified in previous GWAS have been genotyped in ALSPAC. For these analyses we decided *a priori* to use the four SNPs, namely *FTO* (rs9939609), *MC4R* (rs17782313), *TMEM18* (rs6548238) and *GNPDA2* (rs10938397), that had the strongest associations with adiposity in previous studies. ^{14–16} Functional studies are required to ascertain the specific biological pathways through which these polymorphisms affect adiposity. Whilst most pathways to greater adiposity are likely to involve influences on diet/appetite or physical activity, here for the assessment of the IV assumptions (Section 3) we assume that the underlying mechanisms by which they influence diet or physical activity differ for each of the variants under consideration. Although current knowledge about their function is limited, their location on different chromosomes suggests that their influences may indeed be independent. ^{14–16,33,34}

The IV assumptions can be uniquely encoded in a directed acyclic graph (DAG).¹¹ The proposed DAG for our examplar multiple instrument model is shown in Figure 1.

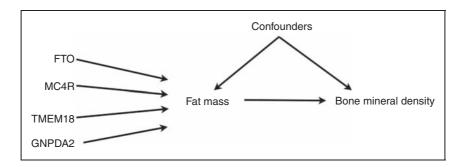


Figure 1. DAG for a Mendelian randomisation analysis using four genetic variants as instrumental variables for the effect of fat mass on bone mineral density.

2.3 Statistical methods

Fat mass and BMD were positively skewed and were log transformed. To account for sex and age differences in fat mass and BMD, age and sex standardised z-scores of log transformed fat mass and BMD were used in the analysis. Genotypes were incorporated into IV models assuming an additive genetic model for the genotypes coded 0, 1 and 2, as shown in Table 1. Height and height-squared were included as covariates in analyses. We exponentiated parameter estimates to derive ratios of geometric mean BMD per standard deviation (SD) increase in log fat mass. Analyses were performed in Stata 11.0.

IV estimation used the two-stage least squares (TSLS) estimator implemented in the user written Stata command ivreg2. ^{35–37} The Hausman test of endogeneity ³⁸ was used to compare the difference between the ordinary-least-squares (OLS) and TSLS estimates using the user-written Stata command ivendog. ³⁵ (In econometrics a risk factor affected by unmeasured confounding factors, such that the assumptions of linear regression are violated, is termed an endogenous variable.) In models including multiple instruments the Sargan test of over-identification (discussed in Section 4.1), available in the ivreg2 command, was used to test the joint validity of the instruments. ³⁹

2.4 Results for separate instruments

Table 1 shows characteristics of the 5 509 eligible children. Of these, 5 091 (92%) had valid genotype data for FTO, 5,412 (98%) for MC4R, 5,323 (97%) for TMEM18, 5 303 (96%) for GNPDA2 and 4 796 (87%) for all four SNPs. Mean age at the time of the DXA scans was 9.9 years. There was no strong evidence against the FTO, TMEM18 and GNPDA2 genotypes being in Hardy-Weinberg

Table 1. Study participant characteristics, total eligible children N = 5509

	N (%)	Mean (SD), geometric mean (95% CI) or N (%)	HWE <i>p</i> -value for genotypes
Gender: N(%) Female	5509 (100%)	2713 (49.3%)	_
Age: Mean (SD) years	5509 (100%)	9.88 (0.32)	
BMD: geometric mean (95% CI) g/cm ²	5509 (100%)	0.902 (0.900, 0.903)	
Fat mass: geometric mean (95% CI) g	5509 (100%)	7209 (7100, 7320)	
Height: mean (SD) cm	5509 (100%)	139.6 (6.3)	
FTO (rs9939609):	5091 (92%)	TT = 0: 868 (37%)	0.51
		TA = I: 2413 (47%)	
		AA = 2: 810 (16%)	
MC4R (rs17782313):	5412 (98%)	TT = 0: 3115 (58%)	0.04
		TC = I: 2017 (37%)	
		CC = 2: 280 (5%)	
TMEM18 (rs6548238):	5323 (97%)	CC = 0: 3705 (70%)	0.57
		CT = I: 1465 (28%)	
		TT = 2: 153 (3%)	
GNPDA2 (rs10938397):	5303 (96%)	AA = 0: 1731 (33%)	0.84
		AG = I: 2604 (49%)	
		GG = 2: 968 (18%)	

HWE: Hardy-Weinberg Equilibrium.

equilibrium. The MC4R genotypes had an Hardy–Weinberg equilibrium p-value of 0.04 in our sample, though in the whole ALSPAC cohort the corresponding p-value was 0.1.

Table 2 shows that there is no strong evidence of associations of the FTO, MC4R or GNPDA2 with height, lean mass, mother's educational achievement and head of household social class. There is some evidence for these data that TMEM18 is associated with lean mass and mother's educational achievement. Under the IV assumptions, TMEM18 genotypes only affect BMD through fat mass; so for now we view these latter two associations as chance findings similar to baseline covariates found to be associated with treatment group in a randomised controlled trial (RCT).

Table 3 shows OLS and IV estimates of the effect of fat mass on BMD in children with complete data. The OLS estimate of the ratio of geometric means per SD increase in log fat mass (adjusted for height and height-squared but not other potential confounders) was 1.22 (95% CI: 1.19, 1.26). The IV estimates of the ratio of geometric means, using each SNP separately, varied between 0.98 (95% CI 0.47–2.03) for *GNPDA2* and 2.33 (1.34–4.05) for *MC4R*. These four IV estimates generally suggest that BMD has a positive effect on fat mass, although the lower limit of the confidence interval for the *TMEM18* estimate and both the lower limit of the confidence interval and point estimate using *GNPDA2* as an instrument, were less than 1. For *MC4R* and *TMEM18*, there was evidence that the IV estimate differed from the OLS estimate, based on the Hausman test of endogeneity (*p*-values 0.006 and 0.089, respectively), with both suggesting a stronger positive association than that found in the OLS analysis.

The first stage R^2 and F-statistics for the instruments based on the explained variation in standardised log fat mass show the expected ranking, with FTO genotype explaining the largest proportion of variation followed by MC4R, TMEM18 and GNPDA2 (these latter two genotypes explained approximately equal variation). The variation in standardised log fat mass explained by each SNP was small, ranging from 0.16% to 0.80%, and the TMEM18 and GNPDA2 SNPs were weak instruments, based on their first-stage F-statistic being less than 10 (Section 4.2). Consistent with the proportion of variation in fat mass explained by each SNP, the standard error (SE) of the IV estimate was smallest for the IV estimate using the FTO SNP (0.16) and largest for TMEM18 and GNPDA2 SNPs (0.43 and 0.37). IV estimates using multiple instruments are described in Section 6.

3 Using multiple instruments to address potential biases in Mendelian randomisation analyses

Population stratification, linkage disequilibrium and pleiotropy have been identified as factors that could bias Mendelian randomisation analyses.^{2,5,11,40} We briefly describe them, and the use of multiple instruments to address issues they raise.

3.1 Population stratification

Population stratification occurs when a sample is composed of a mixture of populations and so contains latent ancestral structure. If there are corresponding differences in the prevalence of the outcome of interest by this structure, then genotype-risk factor associations may result from the presence of ancestrally informative alleles rather than biological function.⁴¹ Some genetic variants that are potential candidates for use as IVs in Mendelian randomisation studies could have been influenced by such population stratification.^{5,42–45} Population stratification therefore has the potential to bias estimates of causal effects in Mendelian randomisation studies.⁵

Table 2. Associations of genotypes with potential confounding factors

			Number of risk alleles		
Genetic var	Genetic variant Covariate (unit) (N)	0	_	2	
Continuous	Continuous confounding factors	Mean (95% CI)	Mean (95% CI)	Mean (95% CI)	Regression coefficient* (95% CI), <i>p-</i> value
FTO	Height (cm) (5091) Lean mass (g) (2515)	139.5 (139.2, 139.7) 24426 (24218, 24634)	139.6 (139.3, 139.8) 24620 (24439, 24800)	139.8 (139.4, 140.3) 24593 (24287, 24899)	0.18 (-0.07, 0.42), $p = 0.165$ 104 (-74, 283), $p = 0.253$
MC4R		139.7 (139.4, 139.9) 24548 (24387, 24708)	139.5 (139.2, 139.8) 24636 (24438, 24834)	140.1 (139.4, 140.9) 24 910 (24 362, 25 458)	0.01 (-0.28, 0.29), $p = 0.965$ 128 (-78, 334), $p = 0.222$
TMEM 18	Height (cm) (5323) Lean mass (g) (2640)	139.7 (139.5, 139.9) 24770 (24622, 24917)	139.5 (139.1, 139.8) 24.286 (24.053, 24.519)	139.3 (138.3, 140.3) 24017 (23.293, 24.740)	$-0.24 \ (-0.56, 0.08), \ p = 0.137$ -447 (-679, -215), $b < 0.001$
GNPDA2	Height (cm) (5303) Lean mass (g) (2625)	139.5 (139.3, 139.8) 24596 (24382, 24810)	139.6 (139.4, 139.9) 24 655 (24 479, 24 832)	139.7 (139.3, 140.1) 24 525 (24 234, 24 816)	0.10 (-0.14, 0.34), $p = 0.420$ -21 (-198, 155), $p = 0.812$
Categorical	Categorical confounding factors	(%) N/u	(%) N/u	n/N (%)	Odds ratio* (95% CI), p-value
FTO	MEA (2421) HHSC (2329)	139/857 (16%)	(%91) 1911/681	69/403 (17%)	1.03 (0.88, 1.20), $p = 0.726$ Chi-squared $p = 0.038$
MC4R	MEA (2591) HHSC (2485)	255/1492 (17%)	(%91) (16%)	25/128 (20%)	0.99 (0.83, 1.18), $p = 0.929$ Chi-squared $p = 0.432$
TMEM 18	MEA (2543) HHSC (2438)	314/1765 (18%)	107/705 (15%)	4/73 (5%)	0.74 (0.60, 0.92), $p = 0.006$ Chi-squared $p = 0.556$
GNPDA2	MEA (2532) HHSC (2432)	151/838 (18%)	203/1236 (16%)	69/458 (13%)	0.90 (0.77, 1.04), $\rho = 0.159$ Chi-squared $\rho = 0.754$
			•		-

MEA: Mother's highest educational achievement is a binary variable derived from the groups 0 = CSE, O-level, Vocational and I = A-level and degree. HHSC: Head of household social class coded as categorical variable I, III III non-manual, III manual, IV and V. *Assuming an additive genetic model.

Table 3. OLS and IV estimates of the effect of fat mass on bone mineral density (BMD) based on complete case analysis, N=4796^a

Method	First stage regression coefficient (95% CI)		First stage F-statistic	First First stage Ratio of geometric mean stage R^2 F-statistic BMD ^b (95% CI)	SE of estimate Hausman (log scale) test <i>p</i> -value	Hausman Sargan test <i>p</i> -value P-value	Sargan test P-value
OLS IV: SNP/s) used as IV	ΝΑ	∢ Z	∀ Z	1.22 (1.19, 1.26), $\rho < 0.001$ 0.014	0.014	N A	∢ Z
FTO	0.11 (0.08, 0.15)	0.0082		1.44 (1.05, 1.97), $p = 0.024$	0.16	0.300	Ϋ́Z
MC4R	0.09 (0.05, 0.13)	0.0037		2.33 (1.34, 4.05), $p = 0.003$	0.28	9000	Ϋ́Z
TMEM 18	-0.06 (-0.11, -0.02)	9100.0		2.27 (0.98, 5.28), $p = 0.056$	0.43	0.089	Ϋ́Z
GNPDA2	0.05 (0.01, 0.09)	9100.0	7.57	0.98 (0.47, 2.03), $p = 0.953$ C	0.37	0.540	Ϋ́Z
FTO, MC4R	AN	0.0119		1.67 (1.27, 2.19), $p < 0.001$	0.14	0.020	0.11
FTO, MC4R, TMEM 18	Ϋ́Z	0.0136		1.73 (1.34, 2.24), $p < 0.001$	0.13	0.010	0.22
FTO, MC4R, TMEM 18, GNPDA2	NA	0.0153		1.63 (1.28, 2.06), $p < 0.001$	0.12	0.013	0.16
Unweighted allele score (4 SNPs)	0.06 (0.04, 0.08)	6900.0		1.40 (0.99, 1.98), $p = 0.055$	0.18	0.430	۲×
Weighted allele score (4 SNPs)	0.19 (0.15, 0.24)	0.0153	74.35	1.63 (1.29, 2.07), $\rho < 0.001$	0.12	0.012	٧Z

^aAnalyses adjusted for height and height squared. ^bFor a 1 unit increase in z-score of age and gender standardised fat mass.

3.2 Linkage disequilibrium

Linkage disequilibrium (LD) is correlation between allelic states at different loci on a stretch of the same chromosome when assessed within a population. LD is a function of the frequency of recombination and is subject to regional genomic characteristics as well as more stochastic processes which may be influenced by the physical distance between two loci as well as the relative age of the population in question. Extensive LD can increase the statistical power of a study to detect genotype-risk factor associations and is exploited in GWAS studies where an LD-based set of tag SNPs is chosen to maximise the amount of genetic variation captured per SNP. SNPs that are associated with phenotypes in GWAS are unlikely to be functional variants, but rather to be in LD with the unknown functional variant(s). According to the functional variant are in LD only with the functional variant(s). However, if tag SNPs are also in LD with a variant that affects the outcome of interest via a pathway that does not include the risk factor of interest the IV assumptions will be violated.

3.3 Pleiotropy

Pleiotropy refers to a single gene having multiple biological functions. In the context of Mendelian randomisation analyses, SNPs in or near genes with pleiotropic effects that directly or indirectly influence the outcome other than through the risk factor of interest violate the IV assumptions. In our example, if any of the adiposity variants had effects on pathways that influence BMD other than through adiposity, for example, if they influenced calcium or vitamin D metabolism, then IV assumptions would not hold.

3.4 Use of multiple instruments

Population stratification and pleiotropy can to some extent be dealt with by using ethnically homogenous study populations, identifying and incorporating population strata in the analysis and ensuring that the function of the genetic instrument is well understood. Comparison of IV estimates based on multiple genetic variants with independent effects on the risk factor of interest provides an additional way to identify bias resulting from these issues. If IV estimates from different variants are similar, it is less plausible that LD or pleiotropy are present.

Comparison of IV estimates from independent genetic variants is analogous to comparing the results of RCTs of different classes of blood pressure lowering drugs, which lower blood pressure by different mechanisms. If the effect of the drug on stroke risk in each RCT is proportional to the direction and magnitude of its effect on blood pressure, this strengthens the evidence for a causal link between blood pressure and stroke risk, and against the drugs having effects on stroke risk through other mechanisms. Such consistency would also argue against the possibility that the trials were affected by methodological flaws that biased their results.

It is possible that separate IV estimates could be identical but biased to a similar extent by population stratification, because stochastic- or selection-driven non-independence that is not predicted by LD profiles could influence more than one genetic variant that affects a given risk factor. Databases such as dbSNP (http://www.ncbi.nlm.nih.gov/projects/SNP/) that provide the fixation index F_{ST} (a measure of population differentiation), or equivalent information, can be used to examine population stratification.

4 Statistical issues relating to use of multiple instruments in Mendelian randomisation analyses

4.1 Over-identification

Over-identification refers to the situation when there is more than one instrument for a single risk factor of interest or, more generally, when there are more instruments than endogenous variables. In such circumstances testing the 'over-identification restriction' checks the joint validity of multiple instruments by testing whether they give the same estimates when used singly or in linear combination. There are two commonly used tests of over-identification; the Hansen test and the Sargan test. ^{39,48} Rejection of an over-identification test is taken to indicate that at least one of the instruments is not valid (i.e., it does not give the same estimate as the other instruments). ⁴⁹

Verifying that the genotypes are independent of the measured confounding factors (Table 2) is an indication of the validity of the instruments.⁵⁰ However, genotypes could still be associated with unmeasured confounders.

4.2 Finite sample bias and instrument strength

IV estimators such as TSLS are asymptotically unbiased but biased in finite samples, with such bias inversely proportional to the amount of phenotypic variability explained by the instrument. Two closely related measures of this are the first-stage regression F-statistic and coefficient of determination R^2 . It is important to report these. If measured confounders are included then the partial R^2 and F-statistics for the instruments should be reported. R^2

In Mendelian randomisation the first stage R^2 is the proportion of risk factor variability explained by genotype. The relationship between the F and R^2 statistics is given by:

$$F = \frac{R^2/k}{(1 - R^2)/(n - k - 1)}. (1)$$

where k is the number of parameters in the model (in this case instruments). The relative bias of the TSLS estimator to the OLS estimator is related to the inverse of the F-statistic. ⁵³ Hahn and Hausman gave a simplified version of the relative bias as approximately the inverse of the F-statistic: ^{54–56}

$$\frac{\text{bias TSLS}}{\text{bias OLS}} \approx \frac{k}{nR^2}$$
 (2)

As R^2 increases the relative bias of TSLS decreases, but including additional instruments that do not increase the first stage R^2 increases the relative bias of TSLS. A first stage F-statistic less than 10 is often taken to indicate a weak instrument, although this is not a strict limit but a rule of thumb drawn from simulation studies. ^{53,57,58} Equation (2) shows that F = 10 corresponds to approximately 10% relative bias. ^{54,58} Alternative IV estimators to TSLS may have better finite sample properties when instruments explain a small proportion of phenotypic variability. ^{59,60}

4.3 Statistical power

Genotypic effects on phenotypes are typically small, so Mendelian randomisation analyses can require very large sample sizes to obtain adequate power.^{5,13} When multiple instruments are used in the TSLS estimator, the resulting IV estimate can be viewed as the efficient linear combination of the separate IV estimates.⁶¹ Provided that each instrument is valid, use of multiple instruments will increase the precision of the IV estimate compared with the separate IV estimates.⁶¹ Donald and

Newey investigated the trade off for multiple instruments where increasing precision can also increase bias, and suggested using the instruments that minimise an approximate mean squared error (MSE) criterion.⁶² Pierce et al. recently estimated the power of Mendelian randomisation studies in a range of settings, using both single and multiple genetic instruments.¹³

In studies where genetic data are not obtained from GWAS (in which imputation based on LD is typically performed) there are typically some missing observations for each genetic variant, due to failure of genotyping or ambiguous genotype allocation. Missing data typically occur in different individuals for each variant. They can therefore result in a considerable cumulative reduction in the number of individuals with complete data on all genotypes, and hence reduce the power of multiple instrument Mendelian randomisation analyses. One approach to dealing with missing data is multiple imputation.⁶³ Whilst there has been considerable research into methods of imputation we are not aware of specific research into appropriate multiple imputation models for IV estimation.

4.4 Use of an allele score as an instrumental variable

An allele score is a weighted or unweighted sum of the number of 'risk' alleles across several genotypes: weights are usually based on each genotype's effect on the phenotype. Use of such scores is becoming more common in gene–disease association studies. ^{64–66} To justify the use of an allele score the genotypes should have an approximately additive effect on the risk factor. For an unweighted score they should also have similar per allele effects.

The use of an allele score as a single IV, compared with multiple instruments, will cause the first stage *F*-statistic to increase, since the number of parameters in the model is reduced. Therefore, the relative bias of the TSLS estimator to the OLS estimator will decrease. However, if the weights are estimated from the same data in which the score is used as an instrument then the single degree of freedom for the allele score *F*-statistic may not be appropriate. When using an allele score the IV estimator is exactly identified, because there is a single instrument and single phenotype, and it is therefore not possible to use an over-identification test for the joint validity of the SNPs.

In general, using an unweighted allele score will have lower power than the multiple instrument approach, since the latter will estimate the efficient linear combination of the genotypes. ⁶¹ Given appropriate weighting, results from IV analyses using weighted allele scores will be similar to the multiple instruments approach.

5 Multiple instrument simulations

We investigated the use of multiple instruments through two simulations both based on our example. Specifically, we investigated bias and precision of IV estimates including: (i) additional non-weak instruments and (ii) weak instruments.

5.1 Simulation I: non-weak instruments

Data were simulated as follows, where G_1 , G_2 and G_3 are genotype variables coded additively, X is the risk factor, Y the disease outcome, U the unmeasured confounder and subscript i denotes a subject:

$$G_{1i} \sim \text{Bin}(2,0.3), G_{2i} \sim \text{Bin}(2,0.3), G_{3i} \sim \text{Bin}(2,0.3), \text{ and,}$$

 $U_i \sim N(0,1),$
 $X_i = 0.55G_{1i} + 0.4G_{2i} + 0.25G_{3i} + U_i \text{ and } Y_i = \beta X_i + U_i.$

The values of the coefficients on the genotypes were chosen so that G_1 explained the most variability in X, followed by G_2 and G_3 . The value of the causal effect of X on Y, β , was set to 1. We monitored the estimates of β from the following models:

- (1) OLS estimate of the regression of Y on X,
- (2) TSLS using G_1 as the instrument,
- (3) TSLS using G_1 and G_2 as instruments,
- (4) TSLS using G_1 – G_3 as instruments,
- (5) TSLS using an unweighted allele score of G_1 – G_3 as an instrument,
- (6) TSLS using a weighted allele score of G_1 – G_3 as an instrument.

We used 10 000 replications, each with a sample size of 5 000 observations. Weighted allele scores were generated by summing each genotype multiplied by its estimated coefficient from the linear regression of the risk factor on that particular genotype, divided by the sum of weights. We derived the average bias, MSE, average SE of the IV estimates, coverage, average R^2 and F-statistics and average absolute TSLS/OLS bias ratio (see Equation (2) in Section 4.2). In a further study we plotted the power curves for models 2–6 for the Wald test of the null hypothesis that $\beta = 1$. For this we used 10 000 replications for values of β in the range 0.8–1.2.

5.2 Simulation I: results

Table 4 shows that the average R^2 values for G_1 , G_1 and G_2 and G_1 — G_3 were 0.12, 0.19 and 0.22, respectively. The average SE decreased by 20% with the inclusion of G_2 and by a further 6% with the inclusion of G_3 .

Models 4 and 6, (multiple instruments using the three genotypes and weighted allele score), had almost identical properties and had the smallest MSE. Model 3 (multiple instruments using G_1 and G_2) had the smallest average bias. The *F*-statistic was greater for the weighted allele score than for the three instrument model (1105 vs. 368) despite having the same average R^2 statistics. This is because the instruments were independent and the weights were derived internally so the weighted score was similar to the linear combination of the instruments derived in the first stage of TSLS.

Figure 2 shows that power increased as the number of instruments increased. The power using the unweighted allele score was similar to that using G_1 and G_2 together, while the power using the weighted allele score was the same as using G_1 – G_3 together.

5.3 Simulation 2: non-weak and weak instruments

Data were simulated with four IVs as follows such that G_1 and G_2 had F-statistics greater than 10 and G_3 and G_4 had F-statistics less than 10. The variables were simulated as: $G_{1i} \sim \text{Bin}(2,0.4)$, $G_{2i} \sim \text{Bin}(2,0.2)$, $G_{3i} \sim \text{Bin}(2,0.2)$, $G_{4i} \sim \text{Bin}(2,0.4)$, and, $U_i \sim N(10,1)$, $X_i = 0.1G_{1i} + 0.1G_{2i} + 0.05G_{3i} + 0.05G_{4i} + U_i$ and $Y_i = \beta X_i + U_i$. The value of the causal effect of X on Y, β , was set to 1. We monitored the estimates of β from the following models:

- (1) OLS estimate from regression of Y on X;
- (2) TSLS estimate using G_1 as the IV;
- (3) TSLS estimate using G_1 and G_2 as the IVs;
- (4) TSLS estimate using G_1 , G_2 , G_3 and G_4 as the IVs;
- (5) TSLS estimate using an unweighted allele score of G_1 and G_2 as the IV;

Table 4. Simulation I (non-weak instruments): results (Monte Carlo standard error reported in brackets beside each estimate)

Model	Average bias	MSE	Average SE	Coverage	Average R ²	Average F	Average absolute TSLS/OLS bias ratio
I. OLS	0.8194 (0.00005)	0.6714 (0.00009)	0.6714 (0.00009) 0.0054 (7E-7) 0	0	ΥN	ΑN	NA
2. TSLS G ₁	-0.0019 (0.0004)	0.0016 (0.00002)	0.0016 (0.00002) 0.03991 (0.00003) 0.9523 (0.0021) 0.1163 (0.0001) 581.41 (0.504)	0.9523 (0.0021)	0.1163 (0.0001)	581.41 (0.504)	0.0022 (0.0005)
3. TSLS G ₁ & G ₂	3. TSLS G ₁ & G ₂ -0.00004 (0.0003)	0.0010 (0.00002)	0.03215 (0.00002)	0.9467 (0.0022)	0.1898 (0.0001)	474.09 (0.333)	0.0001 (0.0004)
4. TSLS G ₁ –G ₃	0.00084 (0.0003)	0.0009 (0.00001)	0.0009 (0.00001) 0.0301 (0.00002) 0.9487 (0.0022) 0.2212 (0.0001) 368.41 (0.243)	0.9487 (0.0022)	0.2212 (0.0001)	368.41 (0.243)	0.0012 (0.0004)
5. TSLS allele	-0.00098 (0.0003)	0.0010 (0.00002)	0.0010 (0.00002) 0.0316 (0.00002)	0.9486 (0.0022)	0.9486 (0.0022) 0.1981 (0.0001) 990.22 (0.685)	990.22 (0.685)	0.0010 (0.0004)
score G_1 – G_3 6. TSLS weighted	0.00084 (0.0003)	0.0009 (0.00001)	0.0009 (0.00001) 0.0301 (0.00002)		0.2212 (0.0001)	0.9492 (0.0022) 0.2212 (0.0001) 1105.43 (0.730) 0.0012 (0.0004)	0.0012 (0.0004)
allele score							
ტ_ს მ_ტ							

MSE: mean squared error, SE: standard error, TSLS: two-stage least squares, OLS: ordinary least squares.

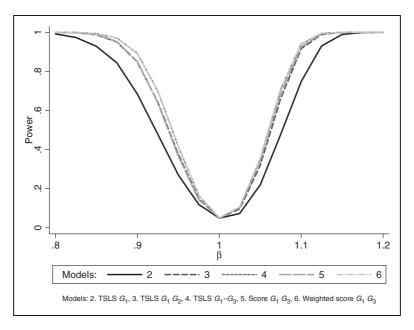


Figure 2. Simulation I (non-weak instruments): power curves.

- (6) TSLS estimate using a weighted allele score of G_1 and G_2 as the IV;
- (7) TSLS estimate using an unweighted allele score of G_1 – G_4 as the IV;
- (8) TSLS estimate using a weighted allele score of G_1 – G_4 as the IV.

We used 10 000 replications, each with a sample size of 5 000 observations. We also plotted power curves for testing β in the range 0 to 2 (again using 10 000 replications for each value of β).

5.4 Simulation 2: results

Table 5 shows that models 3 and 6, using the two non-weak IVs as multiple instruments and just these two in a weighted allele score, had the smallest bias. However, models 4 and 8, using all four genotypes as multiple instruments and all four in the weighted allele score, had the smallest MSE and near identical properties to one another, the only difference being that the average *F*-statistic is larger for the weighted allele score due to its smaller model degrees of freedom. Figure 3 shows that models 4 and 8 also had similar power curves and the largest power of the models considered here. These power curves are asymmetric because the distribution of the estimates was negatively skewed in these simulations.

6 Example revisited: multiple instrument estimates and assessment of missing data

6.1 Multiple instrument estimates

The lower half of Table 3 presents IV estimates using two, three and four genotypes and the unweighted and weighted allele scores. The estimated ratios of geometric means were similar,

Table 5. Simulation 2 (non-weak and weak instruments): results (Monte Carlo standard error in brackets beside each estimate)

							Av. absolute TSLS/OLS
Model	Average bias	MSE	Average SE Coverage	Coverage	Average R ²	Average F	bias ratio
I. OLS	(10000:0) 06:0	0.990 (0.00001) 0.980 (0.00003) 0.0014 (1.9 E-7) 0 (0)	0.0014 (1.9 E-7)	(0) 0	Y Y	ΑN	ΑN
2. TSLS G ₁	-0.047 (0.0025)	0.067 (0.003)	0.237 (0.0015)	0.93 (0.0025)	0.237 (0.0015) 0.93 (0.0025) 0.005 (0.00002) 24.92 (0.099) 0.047 (0.003)	24.92 (0.099)	0.047 (0.003)
3. TSLS G ₁ & G ₂	0.001 (0.0017)	0.028 (0.0006)	0.164 (0.0006)	0.92 (0.0027)	0.164 (0.0006) 0.92 (0.0027) 0.008 (0.00003) 20.99 (0.065) 0.001 (0.002)	20.99 (0.065)	0.001 (0.002)
4. TSLS G ₁ –G ₄	0.040 (0.0013)	0.020 (0.0003)	0.137 (0.0004)	0.89 (0.0031)	0.011 (0.00003)	13.50 (0.036)	0.041 (0.001)
5. TSLS allele score $G_1 \& G_2$	-0.026 (0.0018)	0.032 (0.0007)	0.172 (0.0006)	0.94 (0.0024)	0.172 (0.0006) 0.94 (0.0024) 0.008 (0.00003) 40.99 (0.128) 0.027 (0.002)	40.99 (0.128)	0.027 (0.002)
6. TSLS weighted allele score $G_1 \& G_2$	0.001 (0.0017)	0.028 (0.0006)	0.164 (0.0006)	0.92 (0.0027)	0.164 (0.0006) 0.92 (0.0027) 0.008 (0.00003) 41.99 (0.129) 0.001 (0.002)	41.99 (0.129)	0.001 (0.002)
7. TSLS allele score G ₁ –G ₄	-0.024 (0.0016)	0.027 (0.0006)	0.160 (0.0005)	0.94 (0.0024)	0.160 (0.0005) 0.94 (0.0024) 0.009 (0.00003) 45.91 (0.136) 0.024 (0.002)	45.91 (0.136)	0.024 (0.002)
8. TSLS weighted allele score G ₁ –G ₄	0.040 (0.0013)	0.020 (0.0003)	0.137 (0.0004)	0.89 (0.0031)	0.137 (0.0004) 0.89 (0.0031) 0.011 (0.00003) 54.01 (0.145) 0.041 (0.001)	54.01 (0.145)	0.041 (0.001)

MSE: mean squared error, SE: standard error, TSLS: two-stage least squares, OLS: ordinary least squares.

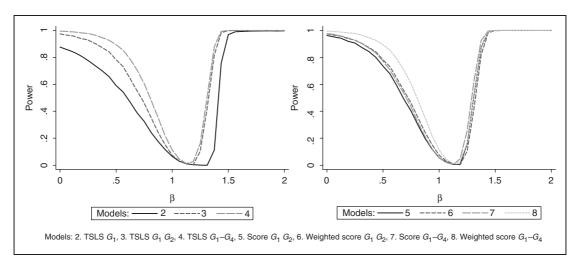


Figure 3. Simulation 2 (non-weak and weak instruments): power curves.

between 1.63 and 1.73, except for the estimate using the unweighted allele score (1.40). Consistent with the simulation studies, the smallest SEs were for the IV estimates using four SNPs and the weighted allele score. For each multiple instrument model, the Sargan over-identification test provides little evidence against the joint validity of the instruments. The Hausman tests suggest that the IV estimates using multiple instruments differ from the OLS estimate.

The SE of the IV estimate using all four SNPs was 0.12, approximately 20% smaller than that of the IV estimate using FTO alone (0.16). As expected, given their low first-stage F-statistics, inclusion of the TMEM18 and GNPDA2 SNPs led only to a small decrease in the SE compared with the multiple instrument model using FTO and MC4R (0.12 compared with 0.14). The IV estimate using all four SNPs had the largest first stage R^2 and smallest SE.

6.2 Assessment of missing data

Table 6 shows IV estimates using the maximum available number of children for each analysis, instead of restricting to children with complete data on all 4 genotypes as in Table 3. Because the sample size increased by only 10–20% for each SNP the SEs of the IV estimates were only slightly smaller than those based on children with complete data. The SE of the IV estimate using all four genotypes as multiple instruments in Table 3 (0.12) was smaller than the SEs of the IV estimates using all available data using one, two and three instruments in Table 6.

7 Discussion and conclusion

Mendelian randomisation studies using genetic variants as instruments can control for unmeasured confounding and reverse causation, which can bias results from standard epidemiological analyses. However, population stratification, LD and pleiotropy can all affect the validity of the IV assumptions underlying Mendelian randomisation analyses. Obtaining similar IV estimates from separate independent instruments provides evidence against the presence of bias from pleiotropy and LD, though not bias from population stratification. In our example there was no evidence that the

Table 6. IV estimates of the effect of fat mass on bone mineral density (BMD) using all available data^a

SNPs used as instrumental variable	z	First stage regression coefficient (95% CI)	First stage R ²	First First stage stage R ² F-statistic	First stage Ratio of geometric F -statistic mean BMD $^{\rm b}$ (95% CI)	SE of estimate (log scale)	Hausman test <i>p</i> -value	Sargan test p-value
OLS	5509	A'N	Ϋ́	ΑN	1.22 (1.18, 1.25), $\rho < 0.001$ 0.014	0.014	ΑN	NA N
IV: SNP(s) used as IV								
FTO	5091	0.12 (0.08, 0.15)	0.0088		1.41 (1.05, 1.89), $p = 0.023$	0.15	0.320	ΑN
MC4R	5412	0.09 (0.05, 0.13)	0.0037		2.42 (1.42, 4.12), $p = 0.001$	0.27	0.002	ΑN
TMEM18	5323	-0.06 (-0.11, -0.02)	0.0013		2.17 (0.92, 5.12), $p = 0.077$	0.44	0.130	Y Y
GNPDA2	5303	0.05 (0.01, 0.08)	0.0013		0.92 (0.42, 2.01), $p = 0.84$	0.40	0.463	ΑN
FTO, MC4R	5007	∀Z	0.0125	31.61	1.60 (1.24, 2.07), $\rho < 0.001$	0.13	0.029	0.221
FTO, MC4R, TMEM18	4881	Ϋ́	0.0138		1.69 (1.32, 2.17), $p < 0.001$	0.13	9000	0.227

^aAnalyses adjusted for height and height squared. ^bFor a 1 unit increase in z-score of age and gender standardised fat mass.

estimates for each instrument differed from each other (based on the over-identification test), providing some reassurance that bias from pleiotropy and LD is unlikely. However, we acknowledge in this example our power to detect differences between the estimates was limited.

Mendelian randomisation analyses require large sample sizes unless the instrument is strongly related to the risk factor (phenotype) of interest. Use of multiple genetic variants as IVs increases the power of such analyses and facilitate tests of the IV assumptions that are not possible in single instrument analyses (such as the test of over-identification). However, inclusion of instruments that explain only a small proportion of the variability in the phenotype can increase finite sample bias of IV estimates. We have limited our consideration to the linear IV model. Non-linear models that naturally arise for discrete outcomes require different treatment.¹¹

Our illustrative Mendelian randomisation analysis confirmed a positive causal effect of adiposity (fat mass) on BMD, in line with previous research ³¹ and suggested that the size of this effect was larger than that estimated by ignoring unmeasured confounding and using ordinary least squares, based on the Hausman endogeneity test. The SE of the IV estimate decreased by around 20% using all four genotypes, compared with the SE of the IV estimate using only the genotype with the strongest effect on risk factor. Such a reduction in SE corresponds to a 56% increase in sample size.

With increasing availability of multiple genetic variants associated with the same risk factor or disease outcome, it is becoming common for genetic association studies to report associations with allele scores. Before an allele score is used as an IV the joint validity of the SNPs should be assessed using an over-identification test. The weights used in weighted allele scores may be internal or external to the study: when internally estimated the single degree of freedom used in the *F*-statistic for instrument strength may not be appropriate. In their simulations Pierce et al. ¹³ used external weights based on the true effect of the genotypes on the phenotype: such weights should be taken from the overall available evidence. They concluded that unweighted and weighted allele scores, using these external weights, decreased bias when compared to the traditional multiple instruments approach, but that they had less power than the multiple instruments approach. In our simulations, models including all instruments, either as multiple instruments or in a weighted allele score, had the greatest power and lowest MSE but not the smallest bias. Based on these results the use of allele scores as IVs can represent a good trade off in terms of lower bias but possibly less precision compared to the TSLS estimator. It has been shown that for larger numbers of IVs, with differing effect sizes, it is better to use a weighted allele score. ¹³

Another consequence of the large number of genetic variants that are being indentified in GWAS in relation to particular phenotypes is that it is possible to generate many independent combinations of such variants and from these many independent IV estimates of the causal effect of a risk factor on a disease outcome. These independent estimates will not be plausibly influenced by any common pleiotropy or LD-induced confounding, and therefore if they display consistency would provide strong evidence against the notion that reintroduced confounding is generating the effect.^{67,68}

There are typically missing data on each genetic variant, due to failure of genotyping or ambiguous genotype allocation. Thus in multiple instrument analyses, missing genotype data can offset improvements in power compared with single instrument analyses. It may be reasonable to assume that the mechanism causing genetic data to be missing is independent of a particular analysis of interest, so this may not be a cause of bias. There is scope for methodological research into multiple imputation strategies for IV estimators. It might also be possible to impute missing data for single SNPs by exploiting the LD structure between SNPs in LD with them, as is common in GWAS. ⁶⁹ In the ALSPAC study, maternal genotypes are available, which could also be used to impute missing offspring genotypes.

In conclusion, the use of multiple genetic instruments increases the statistical power of Mendelian randomisation analyses and provides opportunities to test IV assumptions.

Funding

This work has been funded by a UK Medical Research Council grant (G0601625) entitled 'Inferring epidemiological causality using Mendelian randomization'. DAL, TMP, GDS and NJT work in and RMH, JT and JACS are affiliate members of a UK Medical Research Council Centre (G0600705). The Medical Research Council (MRC), the Wellcome Trust and the University of Bristol provide core funding support for the ALSPAC study. The views expressed in this article are those of the authors and not necessarily those of any funding body or others whose support is acknowledged. The funders had no role in study design, data collection and analysis, decision to publish or preparation of the manuscript.

Acknowledgements

DAL presented parts of this work at the 40th anniversary of the London School of Hygiene & Tropical Medicine MSc in Medical Statistics. The authors would like to thank two anonymous referees and an editorial board member for very helpful comments. We are extremely grateful to all the families who took part in the ALSPAC study, the midwives for their help in recruiting them and the whole ALSPAC team, which includes interviewers, computer and laboratory technicians, clerical workers, research scientists, volunteers, managers, receptionists and nurses.

References

- Youngman LD, Keavney BD, Palmer A, et al. Plasma fibrinogen and fibrinogen genotypes in 4685 cases of myocardial infarction and in 6002 controls: test of causality by 'Mendelian randomization'. Circulation 2000; 102(Supplement II): 31–32.
- Davey Smith G and Ebrahim S. 'Mendelian randomization': can genetic epidemiology contribute to understanding environmental determinants of disease. *Int J Epidemiol* 2003; 32: 1–22.
- 3. Thomas DC and Conti DV. Commentary: the concept of 'Mendelian randomization'. *Int J Epidemiol* 2004; **33**: 21–25.
- Davey Smith G. Capitalising on Mendelian randomization to assess the effects of treatment. James Lind Library, 2006.
- Lawlor DA, Harbord RM, Sterne JAC, Timpson N and Davey Smith G. Mendelian randomization: using genes as instruments for making causal inferences in epidemiology. Stat Med 2008; 27(8): 1133–1163.
- Sheehan NA, Didelez V, Burton PR and Tobin MD. Mendelian randomisation and causal inference in observational epidemiology. *PloS Med* 2008; 5(8): 1205–1210.
- Thanassoulis G and O'Donnell CJ. Mendelian randomization: nature's randomized trial in the post genome era. J Am Med Assoc 2009; 301(22): 2386–2388.
- Thompson JR, Minelli C, Abrams KR, Tobin MD and Riley RD. Meta-analysis of genetic studies using Mendelian randomization-a multivariate approach. Stat Med 2005; 24: 2241–2254.
- Bautista LE, Smeeth L, Hingorani AD and Casas JP. Estimation of bias in non-genetic observational studies using Mendelian triangulation. *Ann Epidemiol* 2006; 16(9): 675–680.

- Thomas DC, Lawlor DA and Thompson JR. RE: Estimation of bias in non-genetic observational studies using 'Mendelian triangulation' by Bautista et al. *Ann Epidemiol* 2007; 17(7): 511–513.
- Didelez V and Sheehan NA. Mendelian randomization as an instrumental variable approach to causal inference. Stat Methods Med Res 2007; 16: 309–330.
- Davey Smith G, Harbord R and Ebrahim S. Fibrinogen, C-reactive protein and coronary heart disease: does Mendelian randomization suggest the associations are non-causal? *QJM* 2004; 97(3): 163–166.
- Pierce BL, Ahsan H and Vanderweele TJ. Power and instrument strength requirements for Mendelian randomization studies using multiple genetic variants. *Int J Epidemiol* 2010; IJE Advance Access published on September 2, 2010.
- Frayling TM, Timpson NJ, Weedon MN, et al. A common variant in the FTO gene is associated with body mass index and predisposes to childhood and adult obesity. *Science* 2007; 316(5826): 889–894.
- Loos RJF, Lindgren CM, Li S, et al. Common variants near MC4R are associated with fat mass, weight and risk of obesity. Nat Genet 2008; 40(6): 768–775.
- Willer CJ, Speliotes EK, Loos RJ, et al. Six new loci associated with body mass index highlight a neuronal influence on body weight regulation. *Nat Genet* 2009; 41(1): 25–34.
- The Wellcome Trust Case Control Consortium. Genomewide association study of 14,000 cases of seven common diseases and 3,000 shared controls. *Nature* 2007; 447(7145): 661–678.

- Sladek R, Rocheleau G, Rung J, et al. A genome-wide association study identifies novel risk loci for type 2 diabetes. *Nature* 2007; 445(7130): 881–885.
- Saxena R, Voight BF, Lyssenko V, et al. Genome-wide association analysis identifies loci for type 2 diabetes and triglyceride levels. *Science* 2007; 316(5829): 1331–1336.
- Scott LJ, Mohlke KL, Bonnycastle LL, et al. A genomewide association study of type 2 diabetes in Finns detects multiple susceptibility variants. *Science* 2007; 316(5829): 1341–1345.
- Lyssenko V, Lupi R, Marchetti P, et al. Mechanisms by which common variants in the TCF7L2 gene increase risk of type 2 diabetes. J Clin Invest 2007; 117(8): 2155–2163.
- Saxena R, Gianniny L, Burtt NP, et al. Common single nucleotide polymorphisms in TCF7L2 are reproducibly associated with type 2 diabetes and reduce the insulin response to glucose in non-diabetic individuals. *Diabetes* 2006; 55(10): 2890–2895.
- Loos RJ, Franks PW, Francis RW, et al. TCF7L2 polymorphisms modulate proinsulin levels and beta-cell function in a British Europid population. *Diabetes* 2007; 56(7): 1943–1947.
- Schafer SA, Tschritter O, Machicao F, et al. Impaired glucagon-like peptide-1-induced insulin secretion in carriers of transcription factor 7-like 2 (TCF7L2) gene polymorphisms. *Diabetologia* 2007; 50(12): 2443–2450.
- Wang J, Kuusisto J, Vanttinen M, et al. Variants of transcription factor 7-like 2 (TCF7L2) gene predict conversion to type 2 diabetes in the Finnish diabetes prevention study and are associated with impaired glucose regulation and impaired insulin secretion. *Diabetologia* 2007; 50(6): 1192–1200.
- Dahlgren A, Zethelius B, Jensevik K, Syvanen AC and Berne C. Variants of the TCF7L2 gene are associated with beta cell dysfunction and confer an increased risk of type 2 diabetes mellitus in the ULSAM cohort of Swedish elderly men. *Diabetologia* 2007; 50(9): 1852–1857.
- Kirchhoff K, Machicao F, Haupt A, et al. Polymorphisms in the TCF7L2, CDKAL1 and SLC30A8 genes are associated with impaired proinsulin. *Diabetologia* 2008; 51(4): 597–601.
- Davey Smith G, Lawlor DA, Harbord R, Timpson N, Day I and Ebrahim S. Clustered environments and randomized genes: a fundamental distinction between conventional and genetic epidemiology. *PloS Med* 2008; 4: e352.
- Angrist JD, Imbens GW and Rubin DB. Identification of causal effects using instrumental variables. *J Am Stat Assoc* 1996; 91(434): 444–455.
- Hernan MA and Robins J. Instruments for causal inference: an epidemiologist's dream? *Epidemiology* 2006; 17: 360–372.
- Timpson NJ, Sayers A, Davey Smith G and Tobias JH. How does body fat influence bone mass in childhood? A Mendelian randomization approach. J Bone Miner Res 2009; 24(3): 522–533.
- Golding J, Pembrey M and Jones R. ALSPAC-the avon longitudinal study of parents and children. I. Study methodology. *Paediatr Perinat Epidemiol* 2001; 15(1): 74–87.
- Gerken T, Girard CA, Tung YC, et al. The obesityassociated FTO gene encodes a 2-oxoglutarate-dependent nucleic acid demethylase. *Science* 2007; 318(5855): 1469–1472.
- Timpson NJ, Emmett PM, Frayling TM, et al. The fat mass-and obesity-associated locus and dietary intake in children. Am J Clin Nutr 2008; 88(4): 971–978.
- Baum CF, Schaffer ME and Stillman S. Instrumental variables and GMM: estimation and testing. *Stata J* 2003; 3(1): 1–32.

 Baum CF, Schaffer ME and Stillman S. Enhanced routines for instrumental variables/generalized method of moments estimation and testing. Stata J 2007; 7(4): 465–506.

- Baum CF, Schaffer ME and Stillman S. 'IVREG2: stata module for extended instrumental variables/2SLS, GMM and AC/HAC, LIML and k-class regression', On line Referencing, [computer program]. http://ideas.repec.org/c/ boc/bocode/s425401.html (2010, accessed November 2010).
- 38. Hausman JA. Specification tests in econometrics. *Econometrica* 1978; **46**(6): 1251–1271.
- Sargan JD. The estimation of economic relationships using instrumental variables. *Econometrica* 1958; 26(3): 393–415.
- Davey Smith G and Ebrahim S. Mendelian randomization: prospects, potentials, and limitations. *Int J Epidemiol* 2004; 33(1): 30–42.
- Cardon LR and Palmer LJ. Population stratification and spurious allelic association. *Lancet* 2003; 361(9357): 598–604.
- Goedde HW, Agarwal DP, Fritze G, et al. Distribution of ADH2 and ALDH2 genotypes in different populations. Hum Genet 1992; 88(3): 344–346.
- 43. Bersaglieri T, Sabeti PC, Patterson N, et al. Genetic signatures of strong recent positive selection at the lactase gene. *Am J Hum Genet* 2004; **74**(6): 1111–1120.
- Wooding S, Kim UK, Bamshad MJ, Larsen J, Jorde LB and Drayna D. Natural selection and molecular evolution in PTC, a bitter-taste receptor gene. Am J Hum Genet 2004; 74(4): 637–646.
- Campbell CD, Ogburn EL, Lunetta KL, et al. Demonstrating stratification in a European American population. *Nat Genet* 2005; 37(8): 868–872.
- Cardon LR and Bell JI. Association study designs for complex diseases. *Nat Rev Genet* 2001; 2(2): 91–99.
- Barrett JC and Cardon LR. Evaluating coverage of genome-wide association studies. *Nat Genet* 2006; 38(6): 659–662.
- Hansen LP. Large sample properties of generalized method of moments estimators. *Econometrica* 1982; 50(4): 1029–1054.
- Cameron AC and Trivedi PK. Microeconometrics using stata. College Station, Texas: Stata Press, 2009.
- 50. Lawlor DA, Timpson N, Harbord RM, et al. Exploring the developmental overnutrition hypothesis using parental-offspring associations and the FTO gene as an instrumental variable for maternal adiposity. The avon longitudinal study of parents and children (ALSPAC). PloS Med 2008; 5: e33.
- Nelson CR and Startz R. Some further results on the exact small sample properties of the instrumental variable estimator. *Econometrica* 1990; 58: 967–976.
- Shea J. Instrument relevance in multivariate linear models: a simple measure. Rev Econ Stat 1997; 79(2): 348–352.
- Staiger D and Stock JH. Instrumental variables regression with weak instruments. *Econometrica* 1997; 65(3): 557–586.
- Bound J, Jaeger DA and Baker RM. Problems with instrumental variables estimation when the correlation between the instruments and the endogenous explanatory variable is weak. J Am Stat Assoc 1995; 90(430): 443–450.
- Hahn J and Hausman JA. Weak instruments: diagnosis and cures in empirical econometrics. Am Econ Rev 2003; 93: 118–125.
- Murray MP. Avoiding invalid instruments and coping with weak instruments. J Econ Perspect 2006; 20: 111–132.
- Cragg JG and Donald SG. Testing identifiability and specification in instrumental variable models. *Economet Theor* 1993; 9: 222–240.
- Stock JH, Wright JH and Yogo M. A survey of weak instruments and weak identification in generalized method of moments. J Bus Econ Stat 2002; 20(4): 518–529.

- Mikusheva A and Poi BP. Tests and confidence sets with correct size when instruments are potentially weak. Stata J 2006; 6(3): 335–347.
- 60. Mikusheva A. Robust confidence sets in the presence of weak instruments. *J Econometrics* 2010; **157**(2): 236–247.
- 61. Wooldridge JM. Econometric analysis of cross section and panel data. Cambridge: Massachusetts: MIT, 2002.
- 62. Donald SG and Newey WK. Choosing the number of instruments. *Econometrica* 2001; **69**(5): 1161–1191.
- 63. Little RJA and Rubin DB. Statistical analysis with missing data. Chichester: Wiley, 2002.
- Weedon MN, McCarthy MI, Hitman GA, et al. Combining information from common Type 2 diabetes risk polymorphisms improves disease prediction. *PloS Med* 2006; 3(10): e374.
- Weedon MN, Lango H, Lindgren CM, et al. Genome-wide association analysis identifies 20 loci that influence adult height. Nat Genet 2008; 40(5): 575–583.

- Lin X, Song K, Lim N, et al. Risk prediction of prevalent diabetes in a Swiss population using a weighted genetic score - the CoLaus study. *Diabetologia* 2009; 52: 600–608
- Davey Smith G. Use of genetic markers and gene-diet interactions for interrogating population-level causal influences of diet on health. *Genes Nutr* 2010; online first doi:10.1007/s12263-010-0181-y.
- Davey Smith G. Mendelian randomization for strengthening causal inference in observational studies: application to gene by environment interaction. *Perspect Psychol Sci* 2010; 5(5): 527–545.
- Marchini J, Howie B, Myers S, McVean G and Donnelly P. A new multipoint method for genome-wide association studies by imputation of genotypes. *Nat Genet* 2007; 39(7): 906–913.